

# SOLUTIONS Assignment #3

①

## Section 1.12 WORD PROBLEMS

# 4

| NAME OF VARIABLE            | UNIT | ORIGINAL BLEND | Added Mix    | FINAL Mix       |
|-----------------------------|------|----------------|--------------|-----------------|
| AMOUNT OF BLEND             | L    | 7600           | $x$          | $7600 + x$      |
| % METHANOL in BLEND         | L/L  | 5%<br>= 0.05   | 50%<br>= 0.5 | 10%<br>= 0.1    |
| AMOUNT OF METHANOL in BLEND | L    | $0.05(7600)$   | $(0.5)x$     | $0.1(7600 + x)$ |

AMOUNT OF METHANOL in ORIGINAL BLEND + AMOUNT OF METHANOL in Added blend = AMOUNT OF METHANOL in FINAL BLEND

$$0.05(7600) + 0.5x = 0.1(7600 + x)$$

$$380 + 0.5x = 760 + 0.1x$$

$$0.4x = 380$$

$$x = 950$$

950 L must be Added.

#16 \* Assume each truck is used once only

| NAME OF VARIABLE      | UNIT     | Fleet A | Fleet B  | TOTAL |
|-----------------------|----------|---------|----------|-------|
| NUMBER OF TRUCKS      | truck    | $x$     | $x+5$    |       |
| HOURS PER TRIP        | hr/truck | 8       | 6        |       |
| TOTAL hrs on delivery | hr       | $8x$    | $6(x+5)$ | 198   |

Hours by Fleet A + Hours by Fleet B = TOTAL hours

$$8x + 6(x+5) = 198$$

$$14x + 30 = 198$$

$$x = 12$$

12 TRUCKS in Fleet A

17 trucks in Fleet B

# 17

Length of MAIN pipeline =  $x$

Length of smaller pipelines =  $x + 2.6$   
(3 OF THEM)

TOTAL length OF 4 pipes = 35.4

$$x + 3(x + 2.6) = 35.4$$

$$x + 3x + 7.8 = 35.4$$

$$4x = 27.6$$

$$x = 6.9$$

So THE MAIN pipeline is 6.9 Km & the smaller ones are 9.5 Km each.

#22

(4)

Let  $x$  = speed of sound

| NAME OF VARIABLE         | UNIT | 1 hour TRIP | 3 hour TRIP | TOTAL TRIP |
|--------------------------|------|-------------|-------------|------------|
| Average speed            | Km/h | $x-100$     | $x+400$     |            |
| Time spent at that speed | h    | 1           | 3           |            |
| distance TRAVELLED       | km   | $1(x-100)$  | $3(x+400)$  | 5740       |

TOTAL distance = distance + distance  
 TRAVELLED ON 1hr Flight ON 3hr Flight

$$5740 = x - 100 + 3(x + 400)$$

$$5740 = x - 100 + 3x + 1200$$

$$4640 = 4x$$

$$x = 1160 \text{ km/hr}$$

#24

Let  $x =$  time until appointment (hr) (5)

| NAME OF VARIABLE   | UNIT | FASTER TRAVELLING     | SLOWER TRAVELLING      |
|--------------------|------|-----------------------|------------------------|
| speed              | Km/h | 60                    | 45                     |
| time travelling    | h    | $x - \frac{1}{6}^*$   | $x - \frac{1}{12}^*$   |
| distance travelled | Km   | $60(x - \frac{1}{6})$ | $45(x - \frac{1}{12})$ |

\* Note  $10 \text{ minutes} = \frac{10}{60} \text{ hrs} = \frac{1}{6}$   
 $5 \text{ minutes} = \frac{5}{60} \text{ hrs} = \frac{1}{12}$

distance travelling FAST = distance travelling SLOW

$$60(x - \frac{1}{6}) = 45(x - \frac{1}{12})$$

$$60x - 10 = 45x - 3.75$$

$$15x = 6.25$$

$$x = \frac{6.25}{15} \text{ hrs}$$

To convert answer to minutes

$$\text{Time until appointment} = \frac{6.25}{15} \cdot 60$$

$$= \boxed{25 \text{ minutes}}$$

#28

| NAME OF VARIABLE     | UNIT | ORIGINAL MIX  | Added Mix   | FINAL MIX            |
|----------------------|------|---------------|-------------|----------------------|
| AMOUNT OF MIX        | L    | $x$           | $8-x$       | 8                    |
| % GAS IN MIX         | L/L  | $75\% = 0.75$ | $100\% = 1$ | $93.75\% = 0.9375^*$ |
| AMOUNT OF GAS IN MIX | L    | $0.75x$       | $1(8-x)$    | $8(0.9375) = 7.5$    |

\*  $\frac{15 \text{ GAS}}{1 \text{ OIL}}$

MEANS  $\frac{15 \text{ (GAS)}}{16 \text{ (TOTAL)}} = 0.9375$   
or 93.75%

GAS IN ORIGINAL MIX + GAS IN Added MIX = GAS IN FINAL MIX

$$0.75x + 8 - x = 7.5$$

$$-0.25x = -0.5$$

$$x = 2$$

2 L OF pure gasoline must be added

#30

| NAME OF VARIABLE       | UNIT       | ROADDED MATERIAL 1 | ROADDED MATERIAL 2 | FINAL MIX        |
|------------------------|------------|--------------------|--------------------|------------------|
| AMOUNT OF MATERIAL     | TONNES (T) | $x$                | $250-x$            | 250              |
| % CRUSHED ROCK         | T/T        | 0.75               | 0.3                | 0.5              |
| AMOUNT OF CRUSHED ROCK | T          | $0.75x$            | $0.3(250-x)$       | $0.5(250) = 125$ |

AMOUNT OF ROCK IN 1 + AMOUNT OF ROCK IN 2 = AMOUNT OF ROCK IN FINAL

$$0.75x + 0.3(250-x) = 125$$

$$0.4x + 75 = 125$$