

Name: \_\_\_\_\_  
Student ID: \_\_\_\_\_

## Test 3

This test is graded out of 48 marks. No books, notes, graphing calculators or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work.

### Question 1.

- a. (2 marks) What angle  $\theta$  ( $0^\circ \leq \theta < 360^\circ$ ) is co-terminal to  $1550^\circ$ .
- b. (2 marks) Consider an angle  $\theta$  in standard position. Then find the quadrant that its terminal edge lies in, if  $\csc \theta < 0$  and  $\cot \theta < 0$ .
- c. (4 marks) Find the values of the other trigonometric functions, if  $\cos \theta = \frac{-1}{2}$  and  $\tan \theta < 0$ .

**Question 2.**

- a. (4 marks) Sketch the graph of  $f(x) = 2^x + 1$ .
- b. (4 marks) Sketch the graph of  $g(x) = \log_{\frac{1}{2}}(x + 1)$
- c. (2 bonus marks) State the domain and range of  $f(x)$  and  $g(x)$ .
- d. (1 bonus mark) Is  $f(x)$  injective, justify.

**Question 3.**

- a. (4 marks) Draw the two “special triangle” which help identify the special angles. Label the angles of the triangles and the lengths of the sides.
- b. (4 marks) Find the exact value of  $\sec 945^\circ$
- c. (4 marks) Find the exact value of  $\cos \frac{4\pi}{3}$

**Question 4.** Solve for  $x$ .

a. (4 marks)

$$2^{2x-1} = 3^{3-x}$$

b. (4 marks)

$$\log_2(x+1) + \log_2(x+4) = 2$$

**Question 5.**

a. (4 marks) Solve the right triangle  $ABC$  ( $C = 90^\circ$ ) given:  $a = 10$ ,  $B = 13^\circ$ .

b. (4 marks) Solve for  $\theta$ , giving the exact solution,  $0^\circ \leq \theta < 360^\circ$

$$\sqrt{3}\sec\theta + 2 = 0$$

**Question 6.** (4 marks) A tree casts a  $20m$  long shadow when the angle of elevation of the sun is  $29^\circ$ . How tall is the tree?

**Bonus.** (3 marks) Solve the triangle  $ABC$  where  $A = 35^\circ$ ,  $a = 70$ ,  $c = 100$ . Do not assume that an angle of the triangle is  $90^\circ$ .