

Quiz 6

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

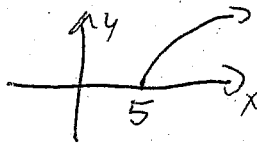
Question 1. pg.75#58 (3 marks) Find $\frac{f(x+h)-f(x)}{h}$ and simplify completely:

$$\begin{aligned}
 f(x) &= \frac{10}{x} + 2 \\
 \frac{f(x+h) - f(x)}{h} &= \frac{\frac{10}{x+h} + 2 - \left[\frac{10}{x} + 2 \right]}{h} \\
 &= \frac{\frac{10}{x+h} - \frac{10}{x}}{h} \\
 &= \frac{\frac{10x - 10(x+h)}{(x+h)x}}{h} \\
 &= \frac{10x - 10x - 10h}{h(x+h)} \\
 &= \frac{-10h}{h(x+h)} \\
 &= \frac{-10\cancel{h}}{\cancel{h}(x+h)} = \frac{-10}{x(x+h)}
 \end{aligned}$$

Question 2. pg.74#32 (2 marks) Determine the domain and range of $y = \sqrt{x-5}$.

$$D: [5, \infty)$$

$$R: [0, \infty)$$



Question 3. pg.90#8g (5 marks) Graph the parabola, noting the intercepts, the vertex, the axis of symmetry, and the range.

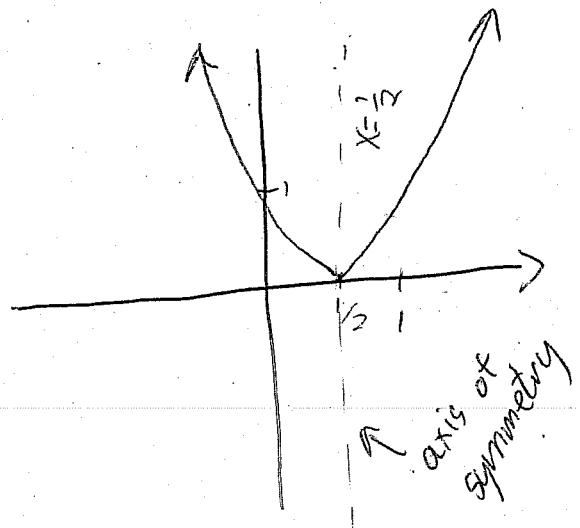
$$f(x) = 4x^2 - 4x + 1$$

$$\begin{aligned}
 f(x) &= 4 \left[x^2 - x + \frac{1}{4} \right] \\
 &= 4 \left[x^2 - x + \frac{1}{4} - \frac{1}{4} + \frac{1}{4} \right] \\
 &= 4 \left[\left(x - \frac{1}{2} \right)^2 + 0 \right] \\
 &= 4 \left(x - \frac{1}{2} \right)^2
 \end{aligned}$$

∴ vertex $\left(\frac{1}{2}, 0 \right)$

y-int: $(0, 1)$

$$\begin{aligned}
 \text{x-int: } 0 &= 4x^2 - 4x + 1 \\
 0 &= (2x-1)^2 \\
 &| \\
 2x-1 &= 0 \\
 x &= \frac{1}{2}
 \end{aligned}$$



Range: $[0, \infty)$