

SOLUTIONS - TEST 2
201-009-50
OCT 2009

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① (a) $(f \circ h)(-3x)$

$$\begin{aligned}
 &= f(h(-3x)) \\
 &= f(-2(-3x)+6) \\
 &= f(6x+6) \\
 &= \frac{3}{6x+6} = \boxed{\frac{1}{2x+2}}
 \end{aligned}$$

(b) $(h \circ g)(t)$

$$\begin{aligned}
 &= h(g(t)) \\
 &= h(-t^2-t) \\
 &= -2(-t^2-t)+6 \\
 &= \boxed{2t^2+2t+6}
 \end{aligned}$$

(c) $(g \circ f)(x)$

$$\begin{aligned}
 &= g(f(x)) \\
 &= g\left(\frac{3}{x}\right) \\
 &= -\left(\frac{3}{x}\right)^2 - \frac{3}{x}
 \end{aligned}$$

$$= \boxed{-\frac{9}{x^2} - \frac{3}{x}}$$

(d) $(f \circ f)(a^2)$

$$\begin{aligned}
 &= f(f(a^2)) \\
 &= f\left(\frac{3}{a^2}\right) \\
 &= \frac{3}{3/a^2} = \boxed{a^2}
 \end{aligned}$$

(e) $(f \circ h \circ g)(2)$

$$\begin{aligned}
 &= (f \circ h)(-2^2-2) \\
 &= (f \circ h)(-6) \\
 &= f(h(-6)) \\
 &= f(-2(-6)+6) \\
 &= f(18) = \frac{3}{18} = \boxed{\frac{1}{6}}
 \end{aligned}$$

② $\frac{a+2}{a-4} + \frac{26-a^2}{12-a^2+a} = \frac{2a-3}{a+3}$

$$\frac{a+2}{a-4} + \frac{26-a^2}{-(a-4)(a+3)} = \frac{2a-3}{a+3}$$

$$\frac{(a+2)(a+3)}{(a-4)(a+3)} - \frac{26-a^2}{(a-4)(a+3)} = \frac{(2a-3)(a-4)}{(a+3)(a-4)}$$

$$\frac{a^2+5a+6-26+a^2}{(a-4)(a+3)} = \frac{2a^2-11a+12}{(a+3)(a-4)}$$

$$2a^2+5a-20 = 2a^2-11a+12$$

$$5a-20 = -11a+12$$

$$16a = 32$$

$$\boxed{a = 2}$$

③ (a) $(-\infty, 4]$ (b) $(1, \infty)$ (c) $\mathbb{R} \setminus \{\pm 7\}$

(d) $h(t) = \sqrt{(t-4)(t-1)}$

	----- ----- -----			
	$(-\infty, 1)$	$(1, 4)$	$(4, \infty)$	
TEST	0	2	5	
SIGN UNDER SQUARE ROOT	+	-	+	DOMAIN
				$(-\infty, 1] \cup [4, \infty)$

④ (a) $y = -3x^2 + 5x + 2$

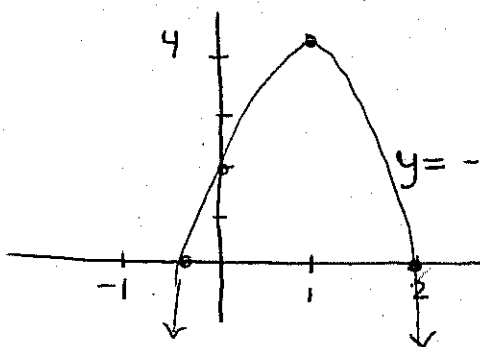
vertex $x = \frac{-b}{2a} = \frac{-5}{2(-3)} = \frac{5}{6}$

$y = -3\left(\frac{5}{6}\right)^2 + 5\left(\frac{5}{6}\right) + 2 = \frac{49}{12}$ $\left(\frac{5}{6}, \frac{49}{12}\right)$

y-intercept $(0, 2)$

x-intercepts

$y = -3x^2 + 6x - x + 2$
 $= -3x(x-2) - 1(x-2)$
 $= (-3x-1)(x-2)$ $x=2$ $x=-\frac{1}{3}$



$y = -3x^2 + 5x + 2$

(b) DOMAIN \mathbb{R}

RANGE $(-\infty, \frac{49}{12}]$

⑤ (a) $h(0) = \boxed{3}$

(b) $0 = -16t^2 + 96t + 3$

$t = \frac{-96 \pm \sqrt{96^2 - 4(-16)(3)}}{2(-16)}$

$= \frac{-96 \pm 97}{-32}$

$t = \boxed{6.03 \text{ s}}$

& $t = -0.03 \text{ s}$
impossible

(c) vertex $t = \frac{-96}{2(-16)} = 3 \text{ s}$

$h(3) = -16(3)^2 + 96(3) + 3 = \boxed{147 \text{ m}}$

$$(6) (a) f(-2) + g(1)$$

$$= (-3(-2)^2 - (-2)) + [2(1) + 7]$$

$$= (-12 + 2) + 9$$

$$= -10 + 9 = \boxed{-1}$$

(3)

$$(b) f(a) + g(a^2)$$

$$= -3a^2 - a + 2a^2 + 7$$

$$= \boxed{-a^2 - a + 7}$$

$$(c) (f \circ g)(3)$$

$$= f(g(3))$$

$$= f(2(3) + 7)$$

$$= f(13)$$

$$= -3(13)^2 - 13$$

$$= \boxed{-520}$$

$$(d) (g \circ f)(3)$$

$$= g(f(3))$$

$$= g(-3(3)^2 - 3)$$

$$= g(-30)$$

$$= 2(-30) + 7$$

$$= \boxed{-53}$$

(7)

$$m = \frac{-2-5}{-3-2} = \frac{-7}{-5} = \frac{7}{5}$$

$$m = \frac{3 - (-1)}{k-4} = \frac{4}{k-4}$$

$$\frac{7}{5} = \text{negative reciprocal}$$

$$\frac{7}{5} = -\left(\frac{k-4}{4}\right)$$

$$\frac{7}{5} = \frac{-k+4}{4}$$

$$28 = -5k + 20$$

$$8 = -5k$$

$$\boxed{k = \frac{8}{-5}}$$

(8)

$$(a) 7x - 32 = 10 - 2(3-x)$$

$$7x - 32 = 10 - 6 + 2x$$

$$5x = 36$$

$$\boxed{x = \frac{36}{5}}$$

$$(c) 4x^2 - 9 = 0$$

$$(2x+3)(2x-3) = 0$$

$$\boxed{x = \pm \frac{3}{2}}$$

$$(b) 5x^2 - 7x - 6 = 0$$

$$5x^2 + 3x - 10x - 6 = 0$$

$$x(5x+3) - 2(5x+3) = 0$$

$$(5x+3)(x-2) = 0$$

$$\boxed{x=2 \quad x = -\frac{3}{5}}$$

$$(d) (3x+4)(x-3) = (x-6)(x+2)$$

$$3x^2 - 5x - 12 = x^2 - 4x - 12$$

$$2x^2 - x = 0$$

$$x(2x-1) = 0$$

$$\boxed{x=0 \quad x = \frac{1}{2}}$$

9. A Line has the FORM $f(x) = mx + b$
TWO POINTS $(2, 1)$ & $(-1, 2)$

$$m = \frac{2-1}{-1-2} = \frac{1}{-3}$$

$$f(x) = -\frac{1}{3}x + b$$

$$2 = -\frac{1}{3}(-1) + b$$

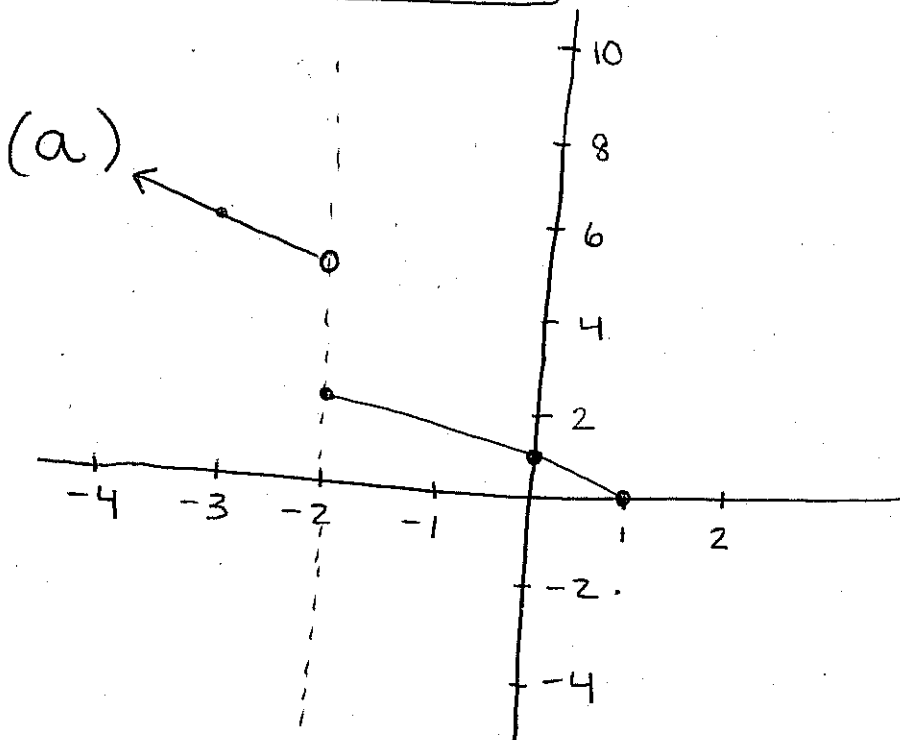
$$2 = \frac{1}{3} + b$$

$$b = \frac{5}{3}$$

$$f(x) = -\frac{1}{3}x + \frac{5}{3}$$

so $f(6) = -\frac{1}{3}(6) + \frac{5}{3}$
= $-\frac{1}{3}$

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$$\sqrt{1-x}$$

x	y
1	0
0	1
-3	2
-8	3
-2	$\sqrt{3} = 1.7$

$$-x+3$$

x	y
-2	5
-3	6
-4	7

(b) Domain

$$(-\infty, 1]$$

RANGE

$$[0, \sqrt{3}] \cup (5, \infty)$$