

NAME SOLUTIONS

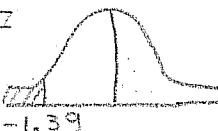
Bonus Exercises – Standard Normal Distribution
201-934-DW Business Statistics
Friday September 25th 2009

1 - Given the standard normal distribution find the following probabilities:

(a) $P(z > -0.1) = 0.5 + 0.0398 = 0.5398$



(b) $P(z < -1.39) = 0.5 - 0.4177 = 0.0823$



(c) $P(-2.04 < z < 0) = 0.4793$

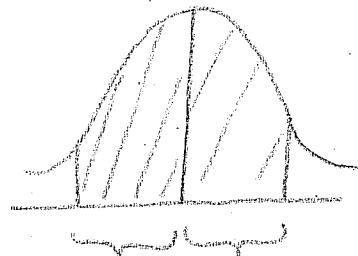
(d) $P(-0.15 < z < 2.1) = 0.0596 + 0.4821 = 0.5417$

(e) $P(0.71 < z < 0.93) = 0.3238 - 0.2611 = 0.0627$

(f) $P(z > 0.78) = 0.5 - 0.2823 = 0.2177$

(g) $P(0 < z < 1.27) = 0.3980$

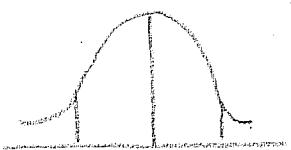
2 - What z values bound the middle 48% of area under the standard normal curve?



24% 24%

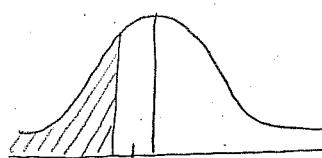
Look up 0.24 in TABLE
(AS AN AREA)

$z = 0.64$



-0.64 0.64

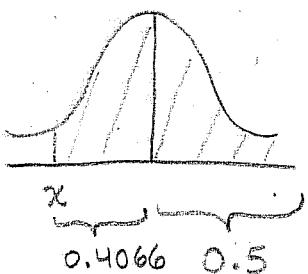
3 - What is the z-score associated with the 42nd percentile of a normal distribution?



$$z = -0.20$$

(Look up 0.08 value
in table as area)

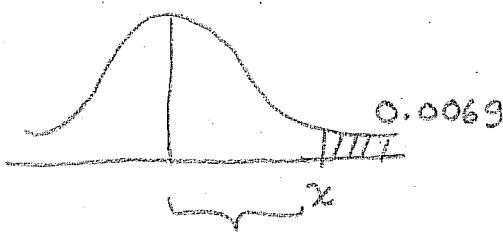
4 – Find the value of x if $P(z > x) = 0.9066$ in the standard normal distribution.



$$x = 1.32$$

$$P(z > 1.32) = 0.9066$$

5 – Find the value of x if $P(z > x) = 0.0069$ in the standard normal distribution.



$$x = 2.46$$

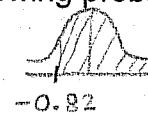
$$P(z > 2.46) = 0.0069$$

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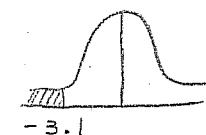
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1 - Given the standard normal distribution find the following probabilities:

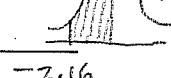
(a) $P(z > -0.82) = 0.5 + 0.2939 = 0.7939$



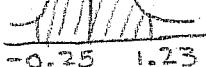
(b) $P(z < -3.1) = 0.5 - 0.4990 = 0.001$



(c) $P(-2.16 < z < 0) = 0.4846$

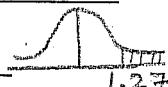


(d) $P(-0.25 < z < 1.23) = 0.0987 + 0.3907 = 0.4894$

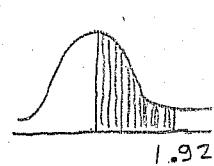


(e) $P(0.54 < z < 1.28) = 0.3997 - 0.2054 = 0.1943$

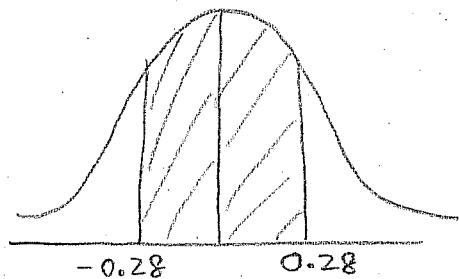
(f) $P(z > 1.27) = 0.5 - 0.3980 = 0.102$



(g) $P(0 < z < 1.92) = 0.4726$



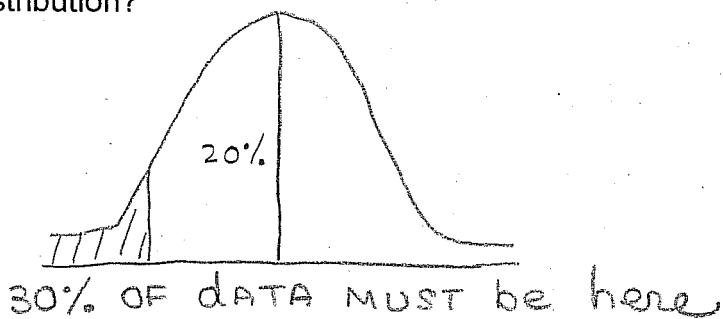
2 - What z values bound the middle 22% of area under the standard normal curve?



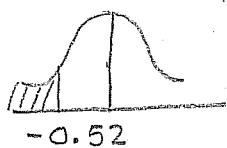
11% 11% Look for z-value closest to 0.11

($z = 0.28$)

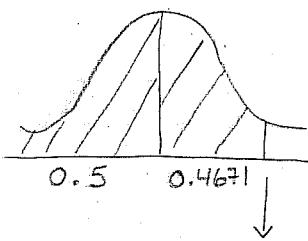
3 - What is the z-score associated with the 30th percentile of a normal distribution?



Look for value close to 0.20
 $(z = 0.52)$



4 - Find the value of x if $P(z < x) = 0.9671$ in the standard normal distribution.

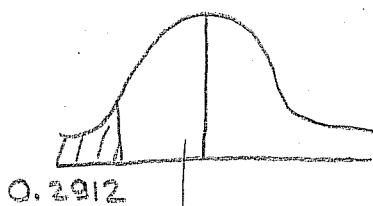


Find z value corresponding
to 0.4671

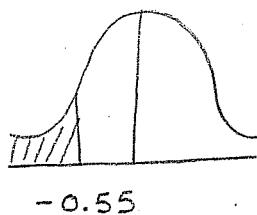
it is 1.84

$$P(z < 1.84) = 0.9671$$

5 - Find the value of x if $P(z < x) = 0.2912$ in the standard normal distribution.



$$\begin{aligned}0.2088 \\ z = 0.55\end{aligned}$$



$$P(z < -0.55) = 0.2912$$

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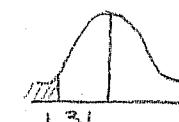
Bonus Exercises – Standard Normal Distribution
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1 - Given the standard normal distribution find the following probabilities:

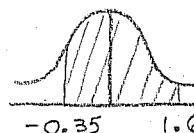
(a) $P(z > -0.23) = \underline{0.5 + 0.0910 = 0.591}$



(b) $P(z < -1.31) = \underline{0.5 - 0.4049 = 0.0951}$



(c) $P(-0.76 < z < 0) = \underline{0.2764}$



(d) $P(-0.35 < z < 1.6) = \underline{0.1368 + 0.4452 = 0.582}$



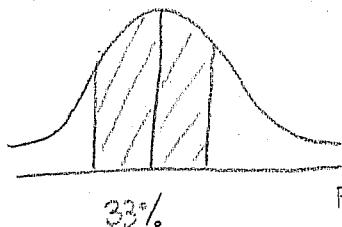
(e) $P(0.75 < z < 1.23) = \underline{0.3907 - 0.2734 = 0.1173}$

(f) $P(z > 2.23) = \underline{0.5 - 0.4871 = 0.0129}$



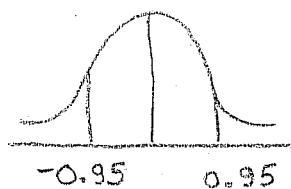
(g) $P(0 < z < 2.16) = \underline{0.4846}$

2 - What z values bound the middle 66% of area under the standard normal curve?

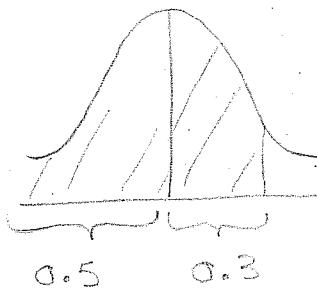


Find 0.33 Area in table

$Z = 0.95$



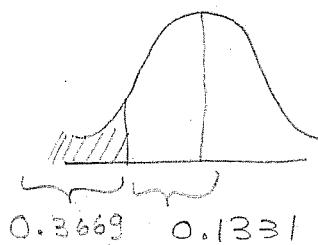
3 - What is the z-score associated with the 80th percentile of a normal distribution?



→ Look up 0.3 Area in TABLE

$$z = 0.84$$

4 – Find the value of x if $P(z < x) = 0.3669$ in the standard normal distribution.



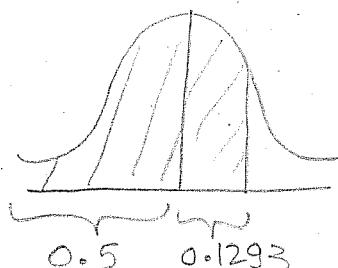
Look up Area of 0.1331
in TABLE

$$z = 0.34$$

$$\text{So } P(z < 0.34) = 0.3669$$

$$x = -0.34$$

5 – Find the value of x if $P(z < x) = 0.6293$ in the standard normal distribution.



Look up Area 0.1293 in
TABLE

$$z = 0.33$$

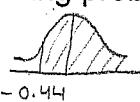
$$P(z < 0.33) = 0.6293$$

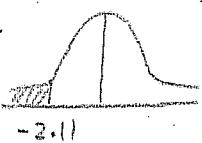
$$\text{So } x = 0.6293$$

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1 - Given the standard normal distribution find the following probabilities:

(a) $P(z > -0.44) = \underline{0.5 + 0.1700 = 0.67}$ 

(b) $P(z < -2.11) = \underline{0.5 - 0.4826 = 0.0174}$ 

(c) $P(-1.76 < z < 0) = \underline{0.4608}$

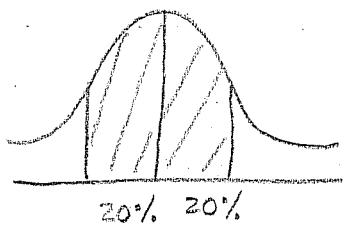
(d) $P(-0.35 < z < 1.1) = \underline{0.1368 + 0.3643 = 0.5011}$

(e) $P(0.25 < z < 1.63) = \underline{0.4484 - 0.0987 = 0.3497}$

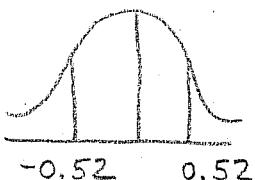
(f) $P(z > 2.2) = \underline{0.5 - 0.4861 = 0.0139}$

(g) $P(0 < z < 2.86) = \underline{0.4979}$

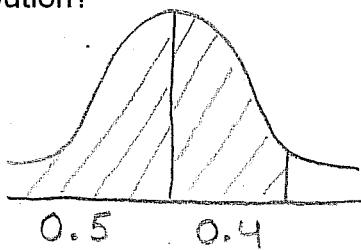
2 - What z values bound the middle 40% of area under the standard normal curve?



Look up 0.20 area
in Table
 $z = 0.52$

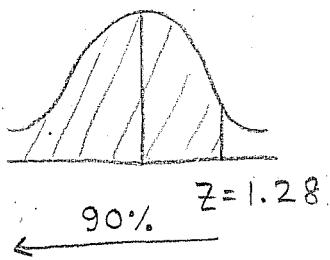


3 - What is the z-score associated with the 90th percentile of a normal distribution?

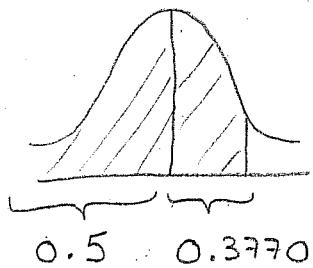


Look up Area 0.4 in table

$$z = 1.28$$



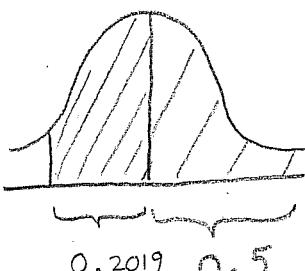
4 - Find the value of x if $P(z < x) = 0.8770$ in the standard normal distribution.



$$x = 1.16$$

$$P(z < 1.16) = 0.8770$$

5 - Find the value of x if $P(z > x) = 0.7019$ in the standard normal distribution.



$$x = -0.53$$

$$P(z > -0.53) = 0.7019$$