

Quiz 7

Question 1. (6 marks) Solve for x:

(a) $x^3 = 10x^2 + 39x$

$$x^3 - 10x^2 - 39x = 0$$

$$x(x^2 - 10x - 39) = 0$$

$$x(x-13)(x+3) = 0$$

$$\begin{array}{ccc} \swarrow & \downarrow & \searrow \\ x=0 & x-13=0 & x+3=0 \\ & x=13 & x=-3 \end{array}$$

$\therefore x = -3, 0, 13$

(b) $(4x-1)(2x-3) = -2$

$$8x^2 - 12x - 2x + 3 = -2$$

$$8x^2 - 14x + 3 + 2 = 0$$

$$8x^2 - 14x + 5 = 0$$

$$8x^2 - 4x - 10x + 5 = 0$$

$$4x(2x-1) - 5(2x-1) = 0$$

$$\begin{array}{ccc} \rightarrow & (4x-5)(2x-1) = 0 & \\ \swarrow & & \searrow \\ 4x-5=0 & & 2x-1=0 \\ 4x=5 & & 2x=1 \\ x=5/4 & & x=1/2 \end{array}$$

$\therefore x = 1/2, 5/4$

CASE 2
 $A \cdot B = 40$
 $A + B = -14$
 $A = -10 \quad B = -4$

Question 2. (4 marks) Find 3 consecutive odd integers such that the product of the first and the third integer is 7 more than 10 times the middle one.

Let x be the first odd integer
 then $x+2$ is the second odd integer
 $x+4$ is the third odd integer

$$x(x+4) = 10(x+2) + 7$$

$$x^2 + 4x = 10x + 20 + 7$$

$$x^2 + 4x = 10x + 27$$

$$x^2 - 6x - 27 = 0$$

$$(x+3)(x-9) = 0$$

$$\begin{array}{ccc} \swarrow & & \searrow \\ x+3=0 & & x-9=0 \\ x=-3 & & x=9 \end{array}$$

THE INTEGERS ARE
 $-3, -1, 1$
 OR
 $9, 11, 13$