

Bonus Quiz 1

This quiz is graded out of 10 marks. No books, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. (2 marks each) Find each limit. Use L'Hôpital's Rule where appropriate. Otherwise elementary method.

a.

$$\lim_{x \rightarrow 3} \frac{2x^2 - 3x - 9}{x^2 - 2x - 3}$$

a) IF $\frac{0}{0}$
 $= \lim_{x \rightarrow 3} \frac{4x - 3}{2x - 2}$ by \hat{H}
 $= \frac{4(3) - 3}{2(3) - 2} = \frac{9}{4}$

b.

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{\sin x}$$

b) IF $\frac{0}{0}$
 $= \lim_{x \rightarrow 0} \frac{\sin x}{\cos x}$ by \hat{H}
 $= \frac{\sin 0}{\cos 0} = \frac{0}{1} = 0$

c.

$$\lim_{x \rightarrow \infty} \frac{\ln(x+1)}{\sqrt{x}}$$

d) $\lim_{x \rightarrow \infty} \frac{\ln(x-10)}{\ln(4x+1)}$ IF $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{1}{\frac{1}{4x+1}}$$
 by \hat{H}

$$= \lim_{x \rightarrow \infty} \frac{4x+1}{4x-10}$$
 IF $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{4}{4}$$
 by \hat{H}

$$= 1$$

d.

$$\lim_{x \rightarrow \infty} \frac{\ln(x-10)}{\ln(4x+1)}$$

e.

$$\lim_{x \rightarrow \infty} \frac{e^{4x}}{e^{3x} + x}$$

e) $\lim_{x \rightarrow \infty} \frac{e^{4x}}{e^{3x} + x}$ IF $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{4e^{4x}}{3e^{3x} + 1}$$
 by \hat{H}

$$= \lim_{x \rightarrow \infty} \frac{16e^{4x}}{9e^{3x}}$$
 IF $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{16e^x}{9} \rightarrow \infty$$

c) $\lim_{x \rightarrow \infty} \frac{\ln(x+1)}{\sqrt{x}}$ IF $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{\frac{1}{x+1}}{\frac{1}{2\sqrt{x}}}$$
 by \hat{H}

$$= \lim_{x \rightarrow \infty} \frac{2\sqrt{x}}{x+1}$$
 IF $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{\frac{1}{\sqrt{x}}}{1}$$
 by \hat{H}

$$= \lim_{x \rightarrow \infty} \frac{1}{\sqrt{x}}$$

$$= 0$$