

## Test 1

The length of the test is 1hr and 45min.

**Question 1. (4 marks)**

Simplify the following expressing your final answer with positive exponents only:

$$\frac{2x^{-2}}{z} \cdot \left( \frac{x^6 y^{-2}}{8x^4 y^9 z^{-3}} \right)^{-1/3} = \frac{2}{x^2 z} \cdot \frac{(x^6)^{-1/3} (y^{-2})^{-1/3}}{(8)^{-1/3} (x^4)^{-1/3} (y^9)^{-1/3} (z^{-3})^{-1/3}}$$

$$= \frac{2}{x^2 z} \cdot \frac{x^{-2} y^{2/3}}{8^{-1/3} x^{-4/3} y^{-3} z} = \frac{2 \cdot 8^{1/3} \cdot y^{2/3} x^{4/3} y^3}{x^2 x^2 z z} = \frac{2 \cdot 2 y^{2/3+3} x^{4/3}}{x^4 z^2}$$

$$= \frac{4 y^{11/3} x^{4/3-4}}{z^2} = \frac{4 y^{11/3}}{x^{8/3} z^2}$$

**Question 2. (6 marks)**

(a) Solve for  $x$ . Express your answer as a fraction:

$$2x - 5 = \frac{5 - 3(4x - 7)}{4}$$

$$4(2x - 5) = 5 - 12x + 21$$

$$8x - 20 = 26 - 12x$$

$$20x = 46$$

$$x = \frac{23}{10}$$

(b) Solve for  $R_1$  in the following equation:

$$P = \frac{QR_1 - R_2(5-u)}{t}$$

$$Pt = QR_1 - R_2(5-u)$$

$$Pt + R_2(5-u) = QR_1$$

$$\frac{Pt + R_2(5-u)}{Q} = R_1$$

**Question 3. (8 marks)**

(a) Find the equation of the line passing through the point  $(-8, 13)$  and parallel to the line  $3 = 5x + 4y$ . Graph this line.

$$4y = -5x + 3$$

$$y = -\frac{5}{4}x + \frac{3}{4}$$

$$\therefore m = -\frac{5}{4}$$

$$y = mx + b$$

$$13 = -\frac{5}{4}(-8) + b$$

$$13 = 10 + b$$

$$3 = b$$

$$\therefore y = -\frac{5}{4}x + 3$$

$$y - mt: x = 0$$

$$y = 3$$

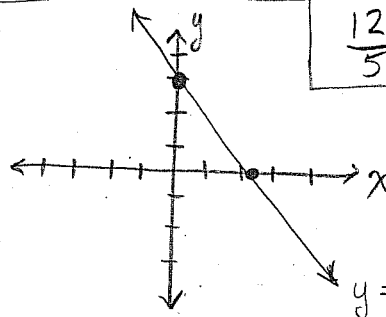
$$(0, 3)$$

$$x - mt: y = 0$$

$$0 = -\frac{5}{4}x + 3$$

$$-3 = -\frac{5}{4}x$$

$$\frac{12}{5} = x, \left(\frac{12}{5}, 0\right)$$



(b) The temperature changes through the wall of a house at a constant rate. The wall is 31cm thick and the temperature is  $24^{\circ}\text{C}$  inside the house. The temperature drops by  $2^{\circ}\text{C}$  for every 3cm moved through the wall from the inside of the house to the outside of the house. Write an equation of the temperature  $T$  as a function of the distance  $x$  from the inside to the outside of the wall. Use this equation to find the temperature outside the house and halfway through the wall.

$$m = \frac{\Delta T}{\Delta x} = -\frac{2}{3}$$

$$\text{AT } x = 0 \quad T = 24$$

$$T = -\frac{2}{3}x + 24$$

OUTSIDE THE HOUSE:

$$T = -\frac{2}{3}(31) + 24 = 3.3^{\circ}\text{C}$$

HALFWAY THROUGH THE WALL:

$$T = -\frac{2}{3}(15.5) + 24 = 13.7^{\circ}\text{C}$$

**Question 4.** (10 marks) (round to 3 significant figures)

(a) Convert  $126 \text{ lbs/in}^3$  to kg per cubic cm.

$$126 \frac{\text{lbs}}{\text{in}^3} \cdot \left( \frac{1 \text{ kg}}{2.20 \text{ lbs}} \right) \cdot \left( \frac{1 \text{ in}}{2.54 \text{ cm}} \right)^3$$
$$= 3.49 \text{ kg/cm}^3$$

(c) Convert  $346 \text{ ft}\cdot\text{lbs}$  (foot pounds) to N·m (Newton metres).

$$346 \text{ ft}\cdot\text{lbs} \cdot \left( \frac{4.45 \text{ N}}{1 \text{ lbs}} \right) \cdot \left( \frac{1 \text{ m}}{3.28 \text{ ft}} \right)$$
$$= 469 \text{ Nm}$$

(d) Convert  $38.2 \text{ Pa}$  to Newtons per square decimetre ( $\text{N/dm}^2$ ).

$$38.2 \text{ Pa} = 38.2 \frac{\text{kg}}{\text{m}\cdot\text{s}^2} = 38.2 \frac{\text{kg}\cdot\text{m}}{\text{s}^2} \cdot \frac{1}{\text{m}^2}$$
$$= 38.2 \frac{\text{N}}{\text{m}^2} = 38.2 \frac{\text{N}}{\text{m}^2} \cdot \left( \frac{10^{-1} \text{ m}}{1 \text{ dm}} \right)^2$$
$$= 0.382 \text{ N/dm}^2$$

**Question 5.** (3 marks) Find the exact values of the following (no decimals or rounding).

(a)  $\cot 30^\circ$

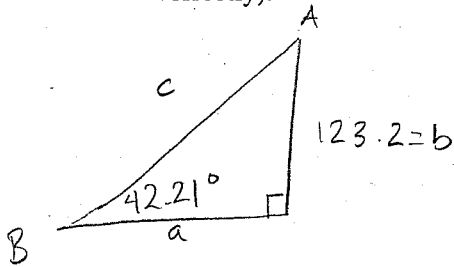
$$\cot 30^\circ = \frac{\cos 30^\circ}{\sin 30^\circ} = \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}} = \sqrt{3}$$

(b)  $\csc(\pi/3)$

$$\frac{\pi}{3} \cdot \frac{180^\circ}{\pi} = 60^\circ$$

$$\csc\left(\frac{\pi}{3}\right) = \csc 60^\circ = \frac{1}{\sin 60^\circ} = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}}$$

**Question 6.** (5 marks) Solve the right triangle with side  $b = 123.2$  and angle  $B = 42.21^\circ$  (round correctly).



$$\sin B = \frac{b}{c} \Rightarrow c = \frac{123.2}{\sin 42.21^\circ} = \underline{183.4}$$

$$a^2 + b^2 = c^2 \Rightarrow a^2 = c^2 - b^2 = 183.3^2 - 123.2^2$$

$$\therefore a = \underline{135.9}$$

$$A = 180^\circ - 42.21^\circ - 90^\circ = \underline{47.79^\circ}$$

**Question 7.** (3 marks) State if the following angles are co-terminal or not.

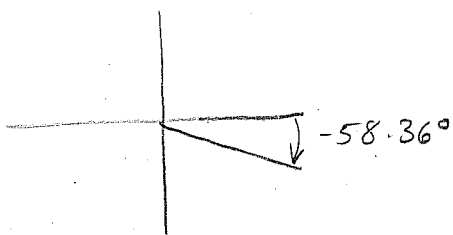
- (a)  $452^\circ$  and  $812^\circ$ . CO-TERMINAL  
 (b)  $862^\circ$  and  $-578^\circ$ . CO-TERMINAL  
 (c)  $197^\circ$  and  $-377^\circ$ . NOT CO-TERMINAL

**Question 8.** (8 marks) Find  $\theta$  given (use the correct number of significant figures):

- (a)  $\tan \theta = -1.623$  and  $0^\circ \leq \theta < 360^\circ$ .

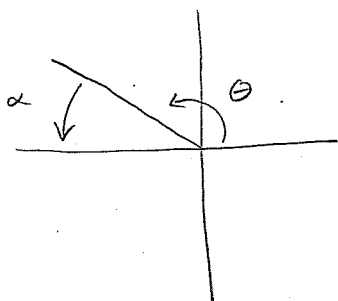
$$\tan^{-1}(-1.623) = -58.36^\circ$$

$\tan \theta < 0 \Rightarrow \theta$  IS IN QUADRANT II OR IV.

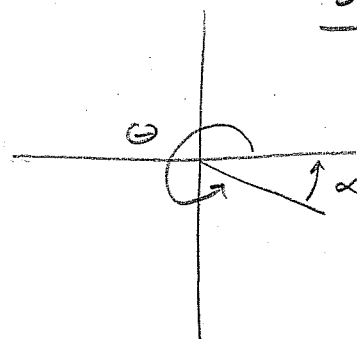


$$\alpha = 58.36$$

QUAD II :  $\theta = 180^\circ - 58.36^\circ = \underline{121.64^\circ}$



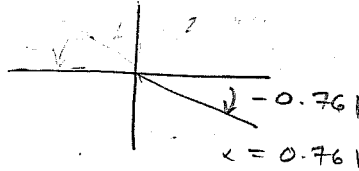
QUAD IV :  $\theta = 360^\circ - 58.36^\circ = \underline{301.64^\circ}$



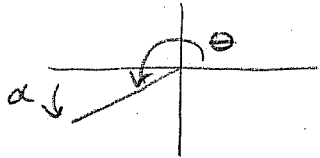
(b)  $\csc \theta = -1.45$ ,  $\tan \theta < 0$  and  $0 \leq \theta < 2\pi$ .

$$\csc \theta = \frac{1}{\sin \theta} = -1.45 \Rightarrow \sin \theta = -\frac{1}{1.45}$$

$$\sin^{-1}\left(-\frac{1}{1.45}\right) = -0.761$$

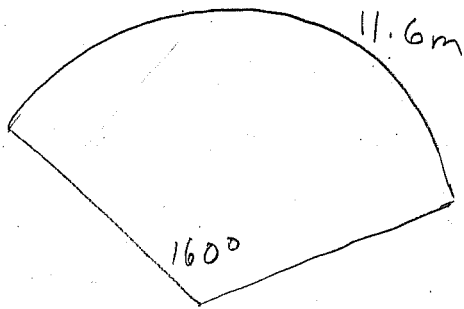


$\sin \theta < 0$  AND  $\tan \theta < 0 \Rightarrow \theta$  IS IN QUADRANT IV



$$\theta = 2\pi - 0.761 = \underline{5.52}$$

**Question 9 (5 marks)** A patio is in the shape of a circular sector with a central angle of  $160^\circ$ . It is enclosed by a railing of which the circular part is 11.6m long. What is the area of the patio?



$$\theta = 160^\circ \cdot \frac{\pi}{180^\circ} = \frac{8\pi}{9}$$

$$\begin{aligned} s &= \theta r \Rightarrow r = \frac{s}{\theta} \\ &= \frac{11.6}{\frac{8\pi}{9}} \\ &= 4.15\text{m} \end{aligned}$$

$$\begin{aligned} A &= \frac{1}{2} \theta r^2 \\ &= \frac{1}{2} \left( \frac{8\pi}{9} \right) (4.15)^2 \\ &= \underline{24.1\text{m}^2} \end{aligned}$$