

Last Name: _____

First Name: _____

Student ID: _____

Assignment

Please attach all work to this assignment. The assignment is due on Tuesday December 7.

For all question circle the letter next to the derivative of f .

1. $f(x) = (x^3 + 2)^2 + x(2 + x)(3x + 5) - x^6$

a. $f'(x) = 12x^2 + 22x + 10$

b. $f'(x) = 21x^2 + 22x + 10$

c. $f'(x) = 12x^3 + 57x^2 + 20$

d. $f'(x) = 21x^2 + 16x + 16$

2. $f(x) = (x^3 - 10x + 5) \left(x^2 - \frac{5}{x} \right)$

a. $f'(x) = 5x^4 + 30x^2 - \frac{25}{x^2}$

b. $f'(x) = (3x^2 - 10)(2x + 5x^{-2})$

c. $f'(x) = 5x^4 - 30x^2 + \frac{25}{x^2}$

d. $f'(x) = \frac{5}{x^{-4}} - 30x^2 - 25x^{-2}$

3. $f(x) = \frac{(3x + 1)^3}{(3x + 2)^3}$

a. $f'(x) = \frac{81x^2 + 54x + 9}{(3x + 2)(3x + 2)^3}$

b. $f'(x) = \frac{9(3x + 1)^2}{(3x + 2)^3}$

c. $f'(x) = \frac{27(3x + 1)^2}{(3x + 2)^2}$

d. $f'(x) = \frac{27(3x + 1)^3}{(3x + 2)^3}$

$$4. f(t) = \frac{(5t^2 + 4)(2t)}{\sqrt[3]{t^4}}$$

$$a. f'(t) = \frac{10t^3 + 8t}{(t^{4/3})^2}$$

$$b. f'(t) = \frac{10t^2 + 4}{t^{-1}/2}$$

$$c. f'(t) = \frac{(30t^{10/3} + 8t^{7/3}) - (\frac{40}{30}t^{10/3} + 16t^{4/3})}{\sqrt[3]{t^4}}$$

$$d. f'(t) = \frac{50t^2 - 8}{3t^{4/3}}$$

$$5. f(x) = \frac{x^2 + 5x}{\sqrt{x^4 + 1}}$$

$$a. f'(x) = \frac{(2x + 5)(x^4 + 1)^{1/2} - 2x^3(x^2 + 5x)}{(x^4 + 1)}$$

$$b. f'(x) = \frac{(2x + 5)(x^4 + 1) - (x^2 + 5x)4x^3}{2(x^4 + 1)^{1/2}(x^4 + 1)}$$

$$c. f'(x) = \frac{2(2x + 5)(x^4 + 1) - 4x^3(x^2 + 5x)}{2(x^4 + 1)^{3/4}}$$

$$d. f'(x) = \frac{-5x^4 + 2x + 5}{x^4 + 1}$$

$$6. f(x) = \frac{(x + 3)^4}{(x^2 + 5)^{1/2}}$$

$$a. f'(x) = \frac{4(x + 3)^3(x^2 + 5)^{1/2} - \left[(x + 3)^4 \cdot \frac{(x^2 + 5)^{1/2}}{2} \cdot (2x) \right]}{(x^2 + 5)}$$

$$b. f'(x) = \frac{(x + 3)^3(3x^2 - 3x + 20)}{(x^2 + 5)^{3/2}}$$

$$c. f'(x) = \frac{(x + 3)^3(3x + 10)(x + 2)}{(x^2 + 5)^{1/2}(x^2 + 5)}$$

$$d. f'(x) = \frac{4(x + 3)^3(x^2 + 5)^{1/2} - \left[(x + 3)^4 \cdot \frac{1}{2(x^2 + 5)^{1/2}} \cdot (2x) \right]}{(x^2 + 5)^{1/2}}$$

$$7. f(x) = \frac{(3x^4 + 4x^3 - 7)^5}{(x^4 + 6x^2 - 6x)^8}$$

$$a. f'(x) = \frac{(x^4 + 6x^2 - 6x)^8 \cdot 5(3x^4 + 4x^3 - 7)^4 \cdot (12x^3 + 12x^2) - (3x^4 + 4x^3 - 7)^5 \cdot 8(x^4 + 6x^2 - 6x)^7 \cdot (4x^3 + 12x - 6)}{(x^4 + 6x^2 - 6x)^{16}}$$

$$b. f'(x) = \frac{(x^4 + 6x^2 - 6x)^8 - 5(3x^4 + 4x^3 - 7)^4 \cdot (12x^3 + 12x^2) - (3x^4 + 4x^3 - 7)^5 - 8(x^4 + 6x^2 - 6x)^7 \cdot (4x^3 + 12x - 6)}{(x^4 + 6x^2 - 6x)^{16}}$$

$$c. f'(x) = \frac{(3x^4 + 4x^3 - 7)^5 \cdot 8(x^4 + 6x^2 - 6x)^7 \cdot (4x^3 + 12x - 6) - (x^4 + 6x^2 - 6x)^8 \cdot 5(3x^4 + 4x^3 - 7)^4 \cdot (12x^3 + 12x^2)}{(x^4 + 6x^2 - 6x)^{16}}$$

$$d. f'(x) = \frac{(x^4 + 6x^2 - 6x)^8 \cdot 5(3x^4 + 4x^3 - 7)^4 \cdot (12x^3 + 12x^2) - (3x^4 + 4x^3 - 7)^5 \cdot 8(x^4 + 6x^2 - 6x)^7 \cdot (4x^3 + 12x - 6)}{(x^4 + 6x^2 - 6x)^{64}}$$

$$8. f(x) = \frac{5x^2 - \pi^3}{\sqrt{2x^3}}$$

$$a. f'(x) = \frac{10x}{2x^3} - \frac{(5x^2 - \pi^3)(6x^2)}{(4x^3)^3/2}$$

$$b. f'(x) = \frac{10x}{2x^3} - \frac{(5x^2 - \pi^3)(6x^2)}{2(2x^3)^3/2}$$

$$c. f'(x) = \frac{5x^2 + 3\pi^3}{2^{3/2}x^{5/2}}$$

$$d. f'(x) = \frac{5x}{x^3} - \frac{(5x^2 - \pi^3)(6x^2)}{2(2x^3)^3/2}$$

$$9. f(x) = \frac{\sqrt{5x^2 + 4x + 8}}{x^2 + 4}$$

$$a. f'(x) = \frac{32x^2 + 16}{(5x^2 + 4x + 8)^{1/2}(x^2 + 4)^2}$$

$$b. f'(x) = \frac{(10x + 4)(x^2 + 4) - 4x(5x^2 + 4x + 8)}{2(5x^2 + 4x + 8)^{1/2}}$$

$$c. f'(x) = \frac{-10x^3 - 12x^2 + 8x + 16}{2(5x^2 + 4x + 8)^{1/2}(x^2 + 4)^2}$$

$$d. f'(x) = \frac{(-10x^3 - 12x^2 + 8x + 16)(x^2 + 4)^2}{2(5x^2 + 4x + 8)^{1/2}}$$

$$10. f(x) = \frac{(x^2 + 7)(2x)}{x}$$

$$\text{a. } f'(x) = 4x^2 - 2$$

$$\text{b. } f'(x) = 2x^3$$

$$\text{c. } f'(x) = 4x^{-2}$$

$$\text{d. } f'(x) = 4x$$

$$11. f(x) = \frac{(5x - 1)(2x^2) - (4x^2 - 6)}{(x + 1)^2}$$

$$\text{a. } f'(x) = \frac{10x^3 + 30x^2 - 12x - 12}{(x + 1)^4}$$

$$\text{b. } f'(x) = \frac{2(x + 1)^3 - 10x^3 + 36x^2 - 12x - 6}{(x + 1)^4}$$

$$\text{c. } f'(x) = \frac{-10x^3 + 36x^2 - 12x - 4}{x + 1}$$

$$\text{d. } f'(x) = \frac{10x^3 + 30x^2 - 12x - 12}{(x + 1)^3}$$

$$12. f(x) = \left[\frac{(x - 7)(x + 3)}{x^2} \right]^5$$

$$\text{a. } f'(x) = 5 \left[\frac{(x - 7)(x + 3)}{x^2} \right]^4 \cdot \frac{-2x^2 + 8x}{x^4}$$

$$\text{b. } f'(x) = \frac{10x(x + 3)^4(x - 7)^4(2x + 21)}{x^{12}}$$

$$\text{c. } f'(x) = \left[\frac{\frac{d}{dx}(x - 7)(x + 3)}{x^2} \right]^5$$

$$\text{d. } f'(x) = 5 \left[\frac{-2x^2 + 8x}{x^4} \right]^4 \frac{4x^5 - 24x^4}{x^8}$$

13. $f(x) = 6x^2 - 8x^2 - \frac{1}{x}$

a. $f'(x) = \frac{12x^3 - 16x^3 + 1}{x^2}$

b. $f'(x) = \frac{-4x^3 - 1}{x^2}$

c. $f'(x) = \frac{4x^3 + 1}{x^2}$

d. $f'(x) = \frac{-4x + 1}{x^2}$

14. $f(x) = \frac{(x+5)(x-2)}{(x^2-1)}$

a. $f'(x) = \frac{-3(x^2 - 6x + 1)}{x^4 - 2x^2 + 1}$

b. $f'(x) = \frac{9x^2 - 22x - 3}{(x^2 - 1)^2}$

c. $f'(x) = \frac{-3(x^2 - 6x + 1)}{x^4 - 1}$

d. $f'(x) = \frac{9x^2 - 22x - 3}{x^4 - 1}$