

Last Name: SOLUTIONS

First Name: _____

Student ID: _____

Quiz 2 (B)

Question 1. (4 marks) Simplify the following expression:

$$\frac{(2x+1)^{1/2} - (x+2)(2x+1)^{-1/2}}{2x+1} = \frac{(2x+1)^{1/2} - \frac{x+2}{(2x+1)^{1/2}}}{2x+1}$$

$$= \frac{(2x+1) - (x+2)}{(2x+1)^{1/2} \cdot 2x+1} = \frac{x-1}{(2x+1)^{1/2} \cdot 2x+1} = \frac{x-1}{(2x+1)^{3/2}}$$

Question 2. (2 marks) Factor the following expression:

$$\begin{aligned} (x-1)^3 - 8 &= [(x-1) - 2][(x-1)^2 + (x-1) \cdot 2 + 2^2] \\ &= (x-3)(x^2 - 2x + 1 + 2x - 2 + 4) \\ &= (x-3)(x^2 + 3) \end{aligned}$$

Question 3. (4 marks) Rationalize the numerator:

$$\begin{aligned} \frac{\sqrt{x+3} - \sqrt{x}}{3} \cdot \frac{\sqrt{x+3} + \sqrt{x}}{\sqrt{x+3} + \sqrt{x}} &= \frac{(x+3) - \sqrt{x}\sqrt{x+3} + \sqrt{x}\sqrt{x+3} - x}{3(\sqrt{x+3} + \sqrt{x})} \\ &= \frac{3}{3(\sqrt{x+3} + \sqrt{x})} = \frac{1}{\sqrt{x+3} + \sqrt{x}} \end{aligned}$$