

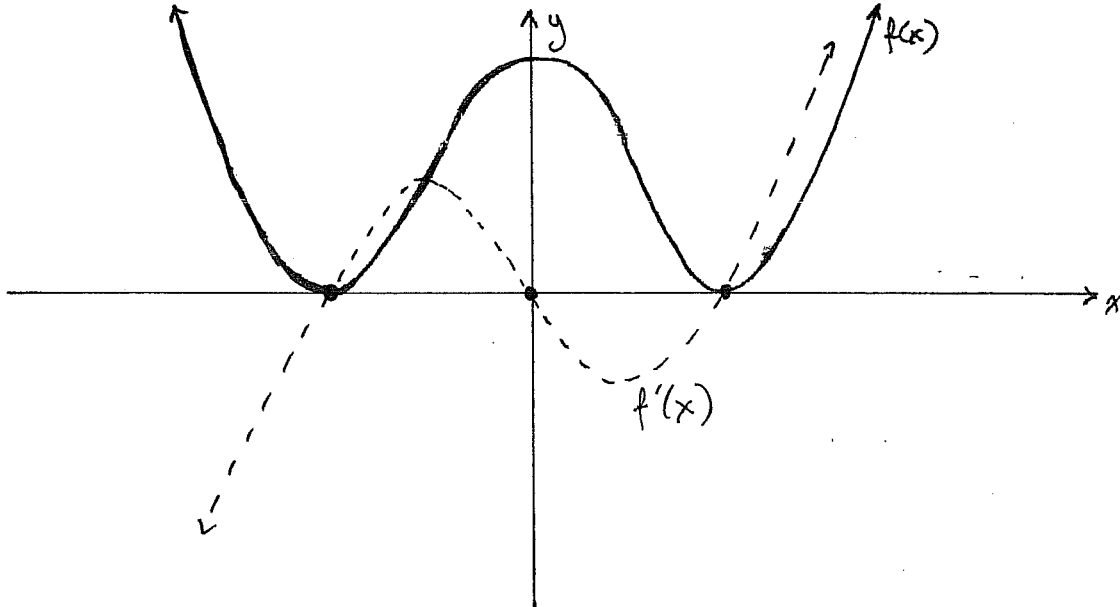
Last Name: SOLUTIONS

First Name: \_\_\_\_\_

Student ID: \_\_\_\_\_

### Quiz 4

Question 1. (5 marks) Sketch the graph of  $f'(x)$  on top of the graph of  $f(x)$  (given below):



Question 2. (5 marks) Find the derivative of the function  $G(t) = \frac{1-2t}{3+t}$  using the definition of the derivative (do not change variables).

$$G'(t) = \lim_{h \rightarrow 0} \frac{G(t+h) - G(t)}{h} = \lim_{h \rightarrow 0} \frac{\frac{1-2(t+h)}{3+(t+h)} - \frac{1-2t}{3+t}}{h} = \lim_{h \rightarrow 0} \frac{\frac{1-2t-2h}{3+t+h} - \frac{1-2t}{3+t}}{h}$$

$$= \lim_{h \rightarrow 0} \frac{(1-2t-2h)(3+t) - (1-2t)(3+t+h)}{(3+t+h)(3+t)h} = \lim_{h \rightarrow 0} \frac{3+t-6t-2t^2-6h-2ht - (3+t+h-6t-2t^2-2ht)}{(3+t+h)(3+t)h}$$

$$= \lim_{h \rightarrow 0} \frac{3+t-6t-2t^2-6h-2ht - 3-t-h+6t+2t^2+2ht}{(3+t+h)(3+t)h} = \lim_{h \rightarrow 0} \frac{-7}{(3+t+h)(3+t)h}$$

$$= \lim_{h \rightarrow 0} \frac{-7}{(3+t+h)(3+t)h} = \frac{-7}{(3+t)(3+t)} = \frac{-7}{(3+t)^2}$$