

Last Name: SOLUTIONS

First Name: _____

Student ID: _____

Quiz 5

Question 1. (4 marks) Find the derivatives of the following functions. You may use any method but remember to use correct notation.

$$(a) y = \frac{x^2 + 4x + 3}{\sqrt{x}} = x^{3/2} + 4x^{1/2} + 3x^{-1/2}$$

$$\therefore y' = \frac{d}{dx}(x^{3/2}) + 4 \frac{d}{dx}(x^{1/2}) + 3 \frac{d}{dx}(x^{-1/2})$$

$$= \frac{3}{2} x^{1/2} + 2 x^{-1/2} - \frac{3}{2} x^{-3/2}$$

$$= \frac{3}{2} x^{1/2} + \frac{2}{x^{1/2}} - \frac{3}{2x^{3/2}}$$

$$(b) H(x) = (x + x^{-1})^3 = (x + x^{-1})(x + x^{-1})(x + x^{-1})$$

$$= (x^2 + 2 + x^{-2})(x + x^{-1}) = x^3 + 2x + x^{-1} + x + 2x^{-1} + x^{-3}$$

$$= x^3 + 3x + 3x^{-1} + x^{-3}$$

$$\therefore H'(x) = \frac{d}{dx}(x^3) + 3 \frac{d}{dx}(x) + 3 \frac{d}{dx}(x^{-1}) + \frac{d}{dx}(x^{-3})$$

$$= 3x^2 + 3 - 3x^{-2} - 3x^{-4}$$

$$= 3x^2 + 3 - \frac{3}{x^2} - \frac{3}{x^4}$$

Question 2. (6 marks) Find an equation of the tangent line to the curve $y = x\sqrt{x}$ that is parallel to the line $y = 1 + 3x$.

$$y = x^{3/2} \Leftrightarrow y' = \frac{3}{2} x^{1/2}$$

SLOPE OF $y = 1 + 3x$ IS $m = 3$ SO THE SLOPE OF OUR TANGENT LINE SHOULD BE THE SAME

$$y' = \frac{3}{2} x^{1/2} = 3 \Leftrightarrow x^{1/2} = 2 \Leftrightarrow x = 4$$

$$\therefore y = 4\sqrt{4} = 8$$

SO THE SLOPE OF THE TANGENT LINE TO $y = x\sqrt{x}$ IS $m = 3$ AT $(4, 8)$.

$$y = mx + b$$

$$8 = 3(4) + b$$

$$-4 = b$$

$$\therefore \boxed{y = 3x - 4} \text{ EQUATION OF TANGENT.}$$