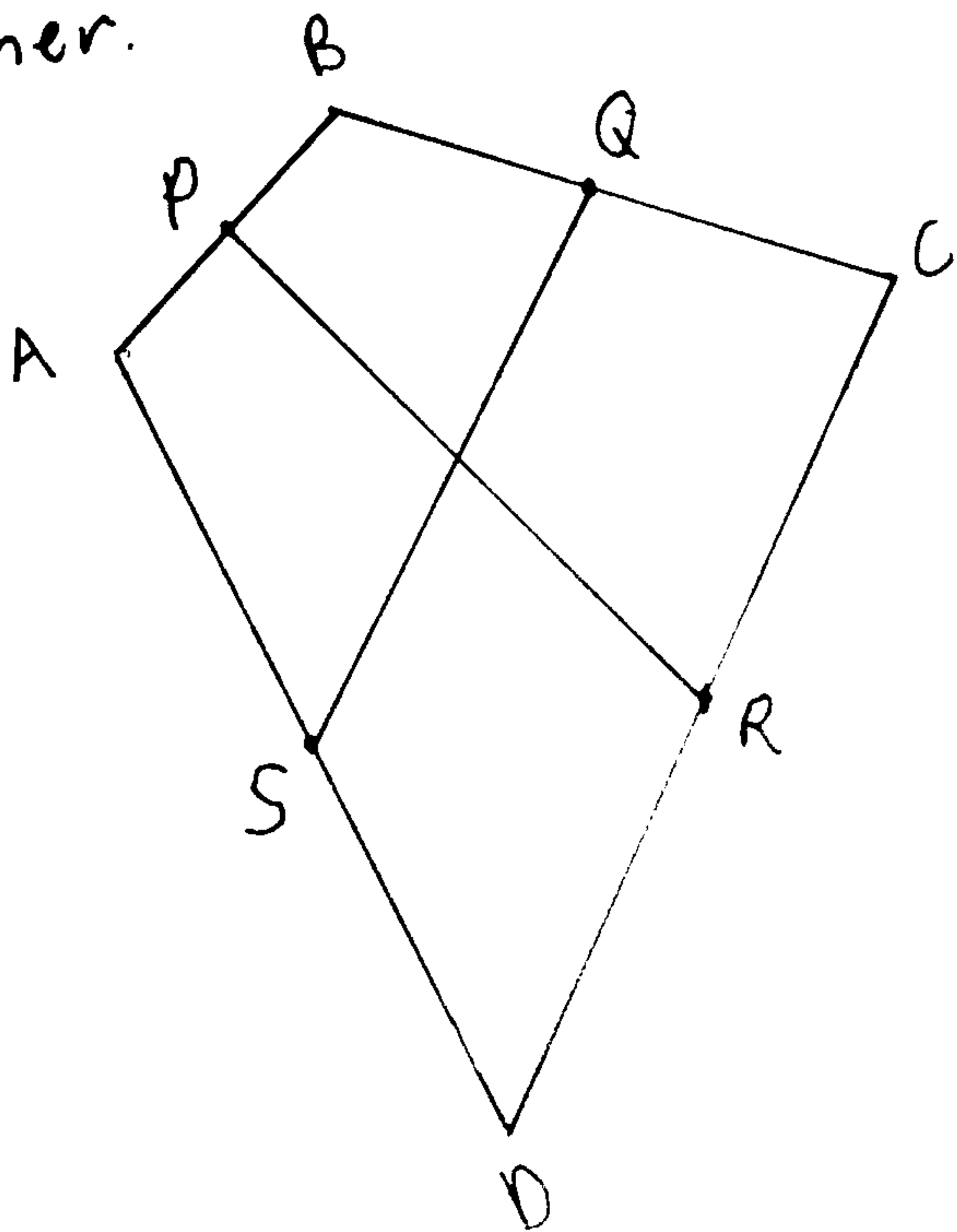


Prove that the line segments joining the midpoints of opposite sides of a quadrilateral bisect each other.



Need to verify that the midpoint of PR is also the midpoint of SQ

$$\vec{OP} = \vec{OA} + \frac{1}{2} \vec{AB}$$

$$P = A + \frac{1}{2} \vec{AB}$$

$$\vec{OR} = \vec{OA} + \vec{AD} + \frac{1}{2} \vec{DC}$$

$$R = A + \vec{AD} + \frac{1}{2} \vec{DC}$$

$$\vec{OQ} = \vec{OA} + \vec{AB} + \frac{1}{2} \vec{BC}$$

$$Q = A + \vec{AB} + \frac{1}{2} \vec{BC}$$

$$\vec{OS} = \vec{OA} + \frac{1}{2} \vec{AD}$$

$$S = A + \frac{1}{2} \vec{AD}$$

Midpoint of PR

$$= \frac{1}{2} (P + R)$$

$$= \frac{1}{2} (A + \frac{1}{2} \vec{AB} + A + \vec{AD} + \frac{1}{2} \vec{DC})$$

$$= \frac{1}{2} (A + \frac{1}{2} (B - A) + A + D + \frac{1}{2} (C - D))$$

$$= \frac{1}{2} (\frac{1}{2} A + \frac{1}{2} B + \frac{1}{2} C + \frac{1}{2} D)$$

Midpoint of SQ

$$= \frac{1}{2} (S + Q)$$

$$= \frac{1}{2} (A + \frac{1}{2} \vec{AD} + A + \vec{AB} + \frac{1}{2} \vec{BC})$$

$$= \frac{1}{2} (A + \frac{1}{2} (D - A) + A + B + \frac{1}{2} (C - B))$$

$$= \frac{1}{2} (\frac{1}{2} A + \frac{1}{2} B + \frac{1}{2} C + \frac{1}{2} D)$$