

[Question 1] A random sample of 200 students are classified below by sex and favourite subject.

Favourite subject	Male	Female
Humanities	34	23
Mathematics	40	41
French	41	21

If a person is picked at random from this group find the probability that:

- The person is female given that their favourite subject is mathematics
- The person is male given that their favourite subject is French.
- The person is female and humanities is their favourite subject.
- The person is male and humanities is their favourite subject.

a. $\frac{41}{81}$

b. $\frac{41}{62}$

c. $\frac{23}{200}$

d. $\frac{34}{200}$

Student Name: _____

SOLUTIONS

[Question 2] The probability that 1st year students pass their mathematics class is 0.7, the probability that 2nd year students pass their mathematics class is 0.5. If a 1st year student has a 0.95 probability of passing his mathematics class if he has a sibling in 2nd year who has passes his mathematics class.

a. Find the probability that a pair of siblings in 1st and 2nd year both pass their mathematics classes given that the 2nd year sibling passed his mathematics class.

b. Find the probability that a 2nd year student passes his mathematics class given that his 1st year sibling has passed his class.

c. At least one member of a pair of siblings passes his mathematics class.

F = FIRST year student
passes

S = Second year student
passes

$$P(F) = 0.7$$

$$P(S) = 0.5$$

$$P(F|S) = 0.95$$

$$\begin{aligned} \text{a. } P(F \cap S) &= P(S)P(F|S) \\ &= (0.5)(0.95) = \underline{0.475} \end{aligned}$$

$$\text{b. } P(S|F) = \frac{P(S \cap F)}{P(F)} = \frac{0.475}{0.7} = \underline{0.679}$$

$$\begin{aligned} \text{c. } P(F \cup S) &= P(F) + P(S) - P(F \cap S) \\ &= 0.7 + 0.5 - 0.475 \\ &= \underline{0.875} \end{aligned}$$