

## Quiz 3

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

**Question 1.** §1.3 #5k (3 marks) Consider the matrices

$$A = \begin{bmatrix} 3 & 0 \\ -1 & 2 \\ 1 & 1 \end{bmatrix}, B = \begin{bmatrix} 4 & -1 \\ 0 & 2 \end{bmatrix}, C = \begin{bmatrix} 1 & 4 & 2 \\ 3 & 1 & 5 \end{bmatrix}, D = \begin{bmatrix} 1 & 5 & 2 \\ -1 & 0 & 1 \\ 3 & 2 & 4 \end{bmatrix}, E = \begin{bmatrix} 6 & 1 & 3 \\ -1 & 1 & 2 \\ 4 & 1 & 3 \end{bmatrix}$$

Compute the given expression (if possible):  $\text{tr}(DE^T)$ .

**Question 2.** §1.3 #TF (2 marks) Determine whether the statement is true or false, and justify your answer.

If  $A$  and  $B$  are square matrices of the same order, then  $\text{tr}(AB) = \text{tr}(A)\text{tr}(B)$ .

**Question 3.** §1.4 #8 (3 marks) Find the inverse of

$$\begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

**Question 4.** §1.4 #TF (2 marks) Determine whether the statement is true or false, and justify your answer.

For all matrices  $A$  and  $B$  of the same size, it is true that  $A^2 - B^2 = (A - B)(A + B)$ .