

Quiz 7

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. §3.2 TF (2 marks) Determine whether the statement is true or false, and justify your answer.

If $\vec{u} \cdot \vec{v} = 0$, then either $\vec{u} = 0$ or $\vec{v} = 0$.

False Let $\vec{u} = (2, 1)$
 $\vec{v} = (-1, 2)$ then $\vec{u} \cdot \vec{v} = 2(-1) + 1(2) = 0$ but $\vec{u} \neq 0$
 $\vec{v} \neq 0$

Question 2. §3.2 #23d (3 marks) Find the cosine of the angle θ between \vec{u} and \vec{v} .

$$\vec{u} = (-2, 2, 3), \vec{v} = (1, 7, -4)$$

$$\vec{u} \cdot \vec{v} = \|\vec{u}\| \|\vec{v}\| \cos \theta$$

$$\vec{u} \cdot \vec{v} = -2(1) + 2(7) + 3(-4) = 0$$

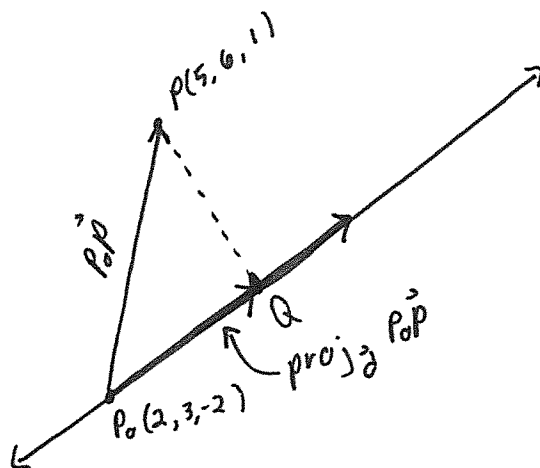
$$0 = \|\vec{u}\| \|\vec{v}\| \cos \theta$$

$$\cos \theta = 0$$

Question 3. 5.22a (5 marks) Find the point on the line which is closest to the point P .

$$x = 2 - t, y = 3 + 2t, z = -2 + t, \text{ and } P(5, 6, 1)$$

$$(x, y, z) = (2 - t, 3 + 2t, -2 + t) = \underbrace{(2, 3, -2)}_{P_0} + t \underbrace{(-1, 2, 1)}_{\vec{d}} \quad t \in \mathbb{R}$$



$$\begin{aligned} \vec{P_0P} &= P - P_0 \\ &= (5, 6, 1) - (2, 3, -2) \\ &= (3, 3, 3) \end{aligned}$$

$$\begin{aligned} P_0Q &= \text{proj}_{\vec{d}} \vec{P_0P} \\ Q - P_0 &= \text{proj}_{\vec{d}} \vec{P_0P} \\ Q &= P_0 + \text{proj}_{\vec{d}} \vec{P_0P} \\ &= (2, 3, -2) + \frac{(3, 3, 3) \cdot (-1, 2, 1)}{(-1, 2, 1) \cdot (-1, 2, 1)} (-1, 2, 1) \\ &= (2, 3, -2) + \frac{6}{6} (-1, 2, 1) \\ &= (1, 5, -1) \end{aligned}$$