Name: _____

Test 3

This test is graded out of 41 marks. No books, notes, unauthorised electronic devices are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1.[1] Let's compare how temperatures have changed in the US from 1968 to 2008. The daily high temperature reading on January 1 was collected in 1968 and 2008 for 51 randomly selected locations in the continental US. Then the difference between the two readings (temperature in 2008 - temperature in 1968) was calculated for each of the 51 different locations. The average of these 51 values was 1.1 degrees with a standard deviation of 4.9 degrees. We are interested in determining whether these data provide strong evidence of temperature warming in the continental US between the years 1968 and 2008.

    a. *(4 marks)* Calculate a 90% confidence interval for the average difference between the temperature measurements between 1968 and 2008.

    b. *(1 mark)* Does the confidence interval provide convincing evidence that the temperature was higher in 2008 than in 1968 in the continental US? Explain.

Question 2. [2] The National Assessment of Educational Progress tested a simple random sample of 1,000 thirteen year old students in both 2004 and 2008 (two separate simple random samples). The average and standard deviation in 2004 were 257 and 39, respectively. In 2008, the average and standard deviation were 260 and 38, respectively.

    a. *(4 marks)* Do these data provide evidence that the average math score for 13 year old students has changed from 2004 to 2008? Use a 10% significance level. *(Write the hypotheses, check conditions, write a conclusion supported by the test statistic)*

    b. *(1 mark)* It is possible that your conclusion in part a. is incorrect. What type of error is possible for this conclusion? What is the probability of committing that type of error? Explain.

Question 3.[3] *(4 marks)* A 90% confidence interval for a population mean is $(65, 77)$. The population distribution is approximately normal and the population standard deviation is unknown. This confidence interval is based on a simple random sample of 25 observations. Calculate the sample mean, the margin of error, and the sample standard deviation. Justify.

Question 4.[4] In a 2010 Survey USA poll, 70% of the 119 respondents between the ages of 18 and 34 said they would vote in the 2010 general election for Prop 19, which would change California law to legalize marijuana and allow it to be regulated and taxed. At a 95% confidence level, this sample has an 8% margin of error. Based on this information, determine if the following statements are true or false.

1. *(1 mark)* There is a 95% probability that between 62% and 78% of the California voters in this sample support Prop 19.
   True or **False**

2. *(1 mark)* We are 95% confident that between 62% and 78% of all California voters between the ages of 18 and 34 support Prop 19.
   True or **False**

3. *(1 mark)* If we considered many random samples of 119 California voters between the ages of 18 and 34, and we calculated 95% confidence intervals for each, 95% of them will include the true population proportion of 18-34 year old Californians who support Prop 19.
   True or **False**

4. *(1 mark)* In order to decrease the margin of error to 4%, we would need to quadruple *(multiply by 4)* the sample size.
   True or **False**

5. *(1 mark)* Based on this confidence interval, there is sufficient evidence to conclude that a majority of California voters between the ages of 18 and 34 support Prop 19.
   True or **False**

Question 5.[5] Among a simple random sample of 331 American adults who do not have a four-year college degree and are not currently enrolled in school, 48% said they decided not to go to college because they could not afford school.

A newspaper article states that only a minority of the Americans who decide not to go to college do so because they cannot afford it and uses the point estimate from this survey as evidence. Conduct a hypothesis test to determine if these data provide strong evidence supporting this statement.

    a. *(1 mark)* Write hypotheses for this research in symbols and in words.

    b. *(1 mark)* Check the conditions required to complete this test.

    c. *(2 marks)* Calculate the test statistic and p-value.

    d. *(1 mark)* What do you conclude at 5% significance? Interpret your conclusion in context.

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e. *(1 mark)* What type of error might we have made? Explain in context what the error means.

f. *(4 marks)* Find an approximation of the propability of the above error given, the hypothesis test at 5% significance and $p_a = 0.45$.

Question 6.[6] According to a report on sleep deprivation by the Centers for Disease Control and Prevention, the proportion of California residents who reported insufficient rest or sleep during each of the preceding 30 days is 8.0%, while this proportion is 8.8% for Oregon residents. These data are based on simple random samples of 11,545 California and 4,691 Oregon residents.

    a. *(5 marks)* Conduct a hypothesis test to determine if these data provide evidence ($\alpha = 0.05$) the rate of sleep deprivation is different for the two states. *(Write the hypotheses, check conditions, write a conclusion supported by the test statistic)*

    b. *(2 marks)* Calculate the margin of error for a 90% confidence interval for the difference between the proportions of Californians and Oregonians who are sleep deprived.

Question 7. *(5 marks)* A 2010 survey asked 827 randomly sampled registered voters in California "Do you support? Or do you oppose? Drilling for oil and natural gas off the Coast of California? Or do you not know enough to say?" Below is the distribution of responses, separated based on whether or not the respondent graduated from college. Complete a chi-square test for these data to check whether there is a statistically significant ($\alpha = 0.05$) difference in responses from college graduates and non-graduates. *(Write the hypotheses, check conditions, write a conclusion supported by the test statistic)*

	College Grad	
	Yes	No
Support	154	132
Oppose	180	126
Do not know	104	131
Total	438	389

Bonus Question. *(3 marks)* Use the flipping a coin analogy to explain what is meant by a 95% confidence interval of a population parameter.