

## Quiz 7

This quiz is graded out of 14 marks. No books, watches, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

**Question 1.** (3 marks) Find  $x$  if the distance between  $(x, 1)$  and  $(2, 5)$  is  $2\sqrt{10}$ .

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$2\sqrt{10} = \sqrt{(2-x)^2 + (5-1)^2}$$

$$(2\sqrt{10})^2 = (\sqrt{(2-x)^2 + 4^2})^2$$

$$4 \cdot 10 = (2-x)^2 + 16$$

$$40 = (2-x)^2 + 16$$

$$24 = (2-x)^2$$

$$\pm\sqrt{24} = 2-x$$

$$x = 2 \pm \sqrt{24}$$

**Question 2.** (1 mark) Find the center of the circle given the 2 endpoints of a diameter:  $(-8, 2)$  and  $(2, 4)$

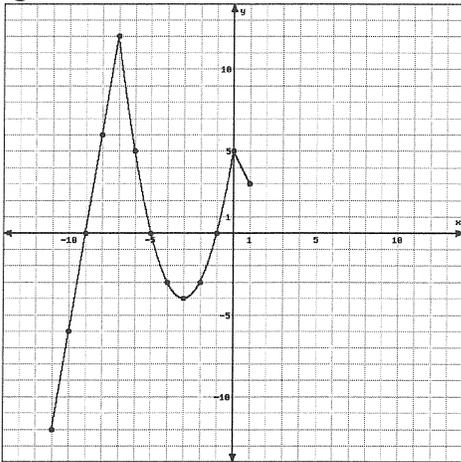


$$M = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \left( \frac{-8+2}{2}, \frac{2+4}{2} \right) = \left( \frac{-6}{2}, \frac{6}{2} \right) = (-3, 3)$$

**Question 3.** (1 mark) Find the radius of the circle whose equation is:  $(x-3)^2 + y^2 = 20$

$$r = \sqrt{20} = \sqrt{4 \cdot 5} = 2\sqrt{5}$$

**Question 4.**



Given the graph of  $y = f(x)$ .

a. (1 mark) State the domain of  $f(x)$ .

$$[-11, 1]$$

b. (1 mark) State the range of  $f(x)$ .

$$[-12, 12]$$

c. (1 mark) Determine  $f(-6)$ .

$$f(-6) = 5$$

d. (1 mark) Determine all  $x$  such that  $f(x) = 0$ .

$$x = -1, -5, -9$$

**Question 5.** (5 marks) Given  $f(x) = \frac{x}{x+1}$ , simplify completely the following expression  $\frac{f(x+h) - f(x)}{h}$ .

$$\frac{f(x+h) - f(x)}{h}$$

$$= \frac{\frac{x+h}{x+h+1} - \frac{x}{x+1}}{h}$$

$$= \frac{\frac{(x+h)(x+1)}{(x+h+1)(x+1)} - \frac{x(x+h+1)}{(x+h+1)(x+1)}}{h}$$

$$= \frac{\frac{(x+h)(x+1) - x(x+h+1)}{(x+h+1)(x+1)}}{h}$$

$$\Rightarrow = \frac{x^2 + x + hx + h - [x^2 + xh + x]}{h(x+h+1)(x+1)}$$

$$= \frac{h}{h(x+h+1)(x+1)}$$

$$= \frac{1}{(x+h+1)(x+1)}$$