

Quiz 9

This quiz is graded out of 14 marks. No books, watches, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. Given $f(x) = -x^2 + 4x - 1$.

- a. (0.5 mark) Find the y-intercept of $f(x)$.

$$(0, f(0)) = (0, -1)$$

- b. (2 marks) Find the x-intercept(s) of $f(x)$, if any.

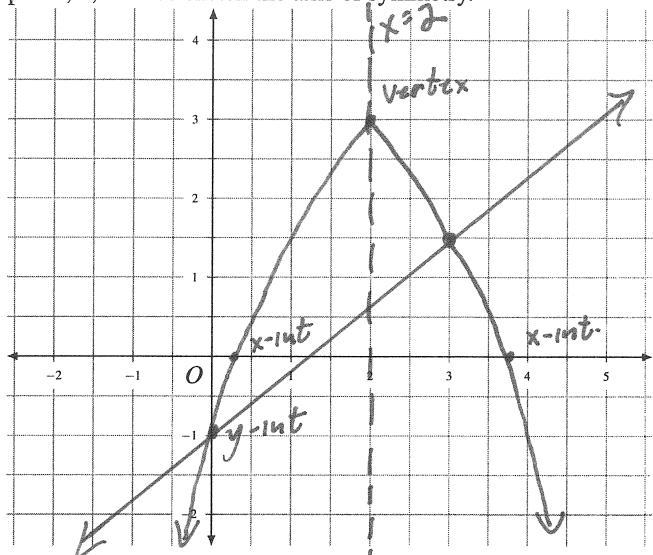
$$\begin{aligned} O &= f(x) \\ 0 &= -x^2 + 4x - 1 \\ x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-4 \pm \sqrt{(4)^2 - 4(-1)(-1)}}{2(-1)} \end{aligned}$$

$$\begin{aligned} &= \frac{-4 \pm \sqrt{12}}{-2} \\ &= \frac{-4 \pm 2\sqrt{3}}{-2} \\ &= 2 \pm \sqrt{3} \\ &\approx 0.27 \text{ and } 3.73 \end{aligned}$$

- c. (1.5 marks) Find the vertex of $f(x)$.

$$\begin{aligned} \left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right)\right) &= (2, -2^2 + 4(2) - 1) \\ = \left(\frac{-4}{2(-1)}, f\left(\frac{-4}{2(-1)}\right)\right) &= (2, 3) \\ = (2, f(2)) & \end{aligned}$$

- d. (4 marks) Sketch the graph and label $f(x)$ and the points found in part a, b, c. Also sketch the axis of symmetry.



- e. (1 mark) State the domain and range of $f(x)$.

Domain: \mathbb{R} Range: $[-\infty, 3]$

Question 2. (5 marks) Find the intersection(s) of the following graphs: $y = -x^2 + 4x - 1$ and $y = x - 1$. Write the intersection(s) as ordered pairs. Sketch the line using the points of intersection(s) on the same axes as Question 1d.

Let's find the intersection of the two graphs

$$\begin{aligned} x - 1 &= -x^2 + 4x - 1 \\ x^2 - 3x &= 0 \\ x(x-3) &= 0 \\ x=0 & \quad x-3=0 \\ x &= 3 \end{aligned}$$

$$x=0: y=0-1=-1$$

∴ intersection at $(0, -1)$

$$x=3: y=3-1=2$$

∴ intersection at $(3, 2)$