

Question 1. (*4 marks each*) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement. Show all your work!

a. There is a basis for M_{22} consisting of invertible matrices.

b. If A has size $n \times n$ and $I_n, A, A^2, \dots, A^{n^2}$ are distinct matrices, then $\{I_n, A, A^2, \dots, A^{n^2}\}$ is a linearly dependent set.

c. There are only three distinct two-dimensional subspaces of P_2 .

d. Every linearly independent subset of a vector space V is a basis for V .