

**Question 1.** (2 marks) A matrix  $B$  is said to be a square root of a matrix  $A$  if  $BB = A$ . Find two square roots of  $A = \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$

**Question 2.** Determine whether the following statements are true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

a. (3 marks) If  $A$  is a square matrix matrix, then  $\text{tr}(A + A^T) = 2\text{tr}(A)$ .

b. (3 marks) If  $A$  and  $B$  are square matrices of the same order, then  $\text{tr}(AB) = \text{tr}(A)\text{tr}(B)$ .

c. (3 marks) If  $B$  has a column of zeros, then so does  $AB$  if this product is defined.

d. (3 marks) If  $AB + BA$  is defined, then  $A$  and  $B$  are square matrices of the same size.