Books, watches, notes or cell phones are not allowed. The only calculators allowed are the Sharp EL-531\*\*. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the world

**Question 1.** (2 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

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If the number of equations in a linear system exceeds the number of unknowns, then the system must be inconsistent.

False, x=1

2x=2 has more egn. than var and has the solution x=1. Hence
it is consistent

**Question 2.** (3 marks) Find all values of k for which the given augmented matrix corresponds to a consistent linear system.

 $\begin{bmatrix} 3 & -4 & k \\ -6 & 8 & 5 \end{bmatrix}$   $\begin{cases} 3x - 4y = K \\ -6x + 8y = 5 \end{cases}$   $\begin{cases} y = \frac{3}{4}x - \frac{K}{4} \\ y = \frac{3}{4}x + \frac{5}{8} \end{cases}$ 

.. both lines are parallel since their slopes are egral. For the system to be consistant the y-intercept must be egral  $\frac{-k}{4} = \frac{5}{8}$   $k = -\frac{5}{2}$ 

Question 2. (3 marks) Given the linear system  $\begin{cases} x - y + z = b_1 \\ 2x - 2y - 2z = b_2. \text{ Determine the } b_i \text{ if the linear system has the particular solution } (3, -2, 1). \\ x + 3y - 5z = b_3 \end{cases}$ 

The solution satisfies the equations ...  $b_1 = 3 - (-2) + 1 = 6$   $b_2 = 2(3) - 2(-2) - 2(1) = 8$  $b_3 = 3 + 3(-2) - 5(1) = -8$ 

**Question 3.** (3 marks) You have a system of k equations in two variables,  $k \ge 2$ . Explain the geometric significance of

a. No solution.

The graphs of the k lines do not have a common point.

b. A unique solution.

The graphs of the k lines have a single point in common

c. An infinite number of solutions.

The graphs of the Klines are identical

**Question 4.** (2 marks) Is there a two-unknowns linear system whose solution set is all of  $\mathbb{R}^2$ ?

Yes, extoy=0 is satisfied by any x, y & R