

Question 1. (2 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If the reduced row echelon form of the augmented matrix for a linear system has a row of zeros, then the system must have infinitely many solutions.

Question 2. (3 marks) The augmented matrix for a system of linear equations has been reduced by row operations to the given row echelon form. Solve the system.

$$\begin{bmatrix} 1 & 2 & 0 & -5 & 6 \\ 0 & 0 & 1 & -9 & 3 \end{bmatrix}$$

Question 3. (5 marks) Determine the values of p for which the system has no solutions, exactly one solution, or infinitely many solutions

$$\begin{array}{rrcrcl} -x & + & 4y & - & 2z & = & 1 \\ -2x & + & 10y & + & (2p-4)z & = & 6 \\ 3x & - & 11y & + & (p^2+6)z & = & 5p-1 \end{array}$$