

Books, watches, notes or cell phones are **not** allowed. The **only** calculators allowed are the Sharp EL-531***. You **must** show all your work, the correct answer is worth 1 mark the remaining marks are given for the work.

Question 1. (3 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If AB and BA are both defined, then AB and BA are square matrices.

Question 2. Find the values of k for which the following system has:

$$\begin{cases} x + y + 2z = -1 \\ -x + (k^2 - 2)y + (2k - 4)z = k + 4 \\ x + y + (k^2 + k)z = k + 1 \end{cases}$$

- Exactly one solution, justify.
- No solutions, justify.
- Infinitely many solutions, justify.

Question 3. (3 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If A and B are square matrices of the same order, then $\text{tr}(AB) = \text{tr}(A)\text{tr}(B)$.

Question 4. (6 marks) Find **all** matrices A , if any, such that A and B commute where $B = \begin{bmatrix} 2 & 3 \\ 5 & 4 \end{bmatrix}$.