

Books, watches, notes or cell phones are **not** allowed. The **only** calculators allowed are the Sharp EL-531***. You **must** show all your work, the correct answer is worth 1 mark the remaining marks are given for the work.

Question 1. (3 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If $AB + BA$ is defined, then A and B are square matrices of the same size.

Question 2. (6 marks) Consider the system

$$\begin{array}{rcl} 2kx + (k+1)y & = & 2 \\ x + y + z & = & 0 \\ kx + (2k-1)y & = & 1 \end{array}$$

Find the value(s) of k , if any, such that the system has:

- no solutions, justify.
- a unique solution, justify.
- infinitely many solutions, justify.

Question 3. (3 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If A and B are square matrices of the same order, then $(AB)^T = A^T B^T$.

Question 3. (6 marks) Find **all** matrices A such that $A \begin{bmatrix} 2 & 3 \\ 5 & 7 \\ -2 & -3 \end{bmatrix} - \begin{bmatrix} 1 \\ 2 \end{bmatrix}^T = \text{trace} \left(\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \right) \begin{bmatrix} 1 \\ 2 \end{bmatrix}^T$.