Question 1. Consider the line (L): $\begin{cases} x = 1 + 2t \\ y = 3 - t \\ z = 5 + t \end{cases}$ where $t \in \mathbb{R}$, the plane (P): x + y - z + 5 = 0, and the point A(4, -2, 5)

a. (5 marks) Using projections find the distance between the line (L) and the plane (P).

b. (1 mark) Find the parametric equation of a line orthogonal to (P) and that passes through A.

c. (4 marks) Find the point on the plane (P) closest to the point A.

d. (1 mark) Find the parametric equation of the plane that contains (L) and is orthogonal to (P).

Question 2. (5 marks) Consider the planes \mathscr{P}_1 : $x + y + z = b_1$ and \mathscr{P}_2 : $x + 2y + cz = b_2$ where b_1, b_2, c are fixed values, P(1, 1, 1) is a point of the intersection between \mathscr{P}_1 and \mathscr{P}_2 and the intersection is parallel to $\mathbf{u} = (2, -1, -1)$.

a. (2 marks) What kind of geometrical object is the intersection of \mathscr{P}_1 and \mathscr{P}_2 , justify.

b. (3 marks) Find the equation of the intersection, as part of your justification use a sketch and state any appropriate theorems.

Question 3. (3 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If **a** and **u** are nonzero vectors, then $\text{proj}_{a}(\text{proj}_{a}(\mathbf{u})) = \text{proj}_{a}(\mathbf{u})$.

Bonus Question. (2 marks) What kind of geometrical object is $r(t) = (t^3, t^3, t^3)$ where $t \in \mathbb{R}$.