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## Test 2

This test is graded out of 60 marks. No books, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

**Question 1.** (1 mark each) Evaluate and round solutions to two decimal places.

a.  $\sqrt[3]{234} \doteq 3.91$

b.  $1.0292^{\frac{49}{9}} \doteq 1.17$

c.  $\ln 231 \doteq 5.44$

d.  $-1^0 = -1$

e.  $(-1)^0 = 1$

**Question 2.** (3 marks) Solve for x.

$$\frac{4}{3}\left(x - \frac{1}{2}\right) - \left(x - \frac{1}{3}\right) = \frac{1}{5} + 10x \quad \text{LCD } 15$$

$$5 \cdot \frac{4}{3} \left(x - \frac{1}{2}\right) - 15 \left(x - \frac{1}{3}\right) = \frac{15}{5} + 15(10x)$$

$$20\left(x - \frac{1}{2}\right) - 15x + \frac{15}{3} = 3 + 150x$$

$$20x - \frac{20}{2} - 15x + 5 = 3 + 150x$$

$$20x - 10 - 15x + 5 = 3 + 150x$$

$$-8 = 145x$$

$$x = \frac{-8}{145}$$

**Question 3.** (3 marks) Expand and simplify.

$$(x-2)^2 - (x-3)(x-4)$$

$$= [x^2 - 4x + 4] - [x^2 - 4x - 3x + 12]$$

$$= x^2 - 4x + 4 - x^2 + 7x - 12$$

$$= 3x - 8$$

Question 4. (3 marks) Simplify.

$$\begin{aligned}\frac{(3x^2y^{-3})^4}{(2x^{\frac{1}{2}}y^5)^{-2}} &= \frac{3^4(x^2)^4(y^{-3})^4}{2^{-2}(x^{\frac{1}{2}})^{-2}(y^5)^{-2}} \\ &= \frac{3^4 x^8 y^{-12}}{4^{-1} x^{-1} y^{-10}} \\ &= \frac{324 x^9}{y^2}\end{aligned}$$

Question 5. (3 marks) Isolate  $i$ .

$$\begin{aligned}FV &= PV(1+i)^n \\ \frac{FV}{PV} &= (1+i)^n \\ \sqrt[n]{\frac{FV}{PV}} &= 1+i \\ \sqrt[n]{\frac{FV}{PV}} - 1 &= i\end{aligned}$$

Question 6. (4 marks) Karl has a gross salary for the week of \$538.38. He receives a base salary of \$300 and has 7.2% commission on his net sales with a quota of \$3 000. What were his net sales for the week?

$$\begin{aligned}\text{Portion of salary that is from commission} &= 538.38 - 300 \\ &= 238.58\end{aligned}$$

$$\begin{aligned}\text{net sales} &= 3000 + \frac{238.58}{0.072} \\ &= \$6313.61\end{aligned}$$

**Question 7.** (2 marks) The City of Atwater has announced that this year's mill rate has been set at 55.38. Noam has a property assessed at \$320 000, what amount will he pay this year in property taxes?

$$\begin{aligned}\text{Property tax} &= \frac{\text{Mill rate}}{1000} \times (\text{assessed value}) \\ &= \frac{55.38}{1000} (320\,000) \\ &= \$ 17\,721.60\end{aligned}$$

**Question 8.** (3 marks) Solve for x.

$$3 : 8 = 21 : x$$

$$\frac{3}{8} = \frac{21}{x}$$

$$3x = 21(8)$$

$$x = \frac{21(8)}{3}$$

$$x = 7(8)$$

$$x = 56$$

**Question 9.** (4 marks) The component cost to make an OGG Vorbis player is four-seventh of the total cost, and labour is one-third of the component cost. If cost of labour is \$11 what is the total cost of the OGG Vorbis player.

$$\frac{\text{components}}{\text{Cost}} = \frac{4}{7}$$

$$\frac{\text{labour}}{\text{component}} = \frac{1}{3}$$

$$\frac{11}{\text{component}} = \frac{1}{3}$$

$$\$ 33 = \text{component}$$

$$\text{Cost} = \frac{7 \text{ component}}{4}$$

$$= \frac{7(33)}{4} = \$ 57.75$$

**Question 10.** (2 marks) What is 35% of \$233?

$$\begin{aligned}\text{Percentage} &= \text{base} \times \text{rate} \\ &= 233 (0.35) \\ &= \$81.55\end{aligned}$$

**Question 11.** (2 marks) \$300 is 15% of what amount?

$$\begin{aligned}\text{Percentage} &= \text{base} \times \text{rate} \\ 300 &= \text{base} (0.15) \\ \$2000 &= \text{base}\end{aligned}$$

**Question 12.** (2 marks) If \$124.24 is the amount after GST, what was the amount before GST?

$$\begin{aligned}1.05 (\text{before GST}) &= \text{after GST} \\ \text{before GST} &= \frac{124.24}{1.05} \\ &= \$118.32\end{aligned}$$

**Question 13.** (4 marks) A computer is sold to a retailer for \$399.99 less 25%, 15%, 5%. What is the net price? What is the total discount? What is the single rate of discount?

$$\begin{aligned}n &= (1-d_1)(1-d_2)(1-d_3)L \\ &= (1-0.25)(1-0.15)(1-0.05) 399.99 \\ &= \$242.24\end{aligned}$$

$$\begin{aligned}\text{Total discount} &= 399.99 - 242.24 \\ &= \$157.75\end{aligned}$$

$$\begin{aligned}\text{Single rate of discount} &= 1 - [(1-d_1)(1-d_2)(1-d_3)] \\ &= 1 - [(1-0.25)(1-0.15)(1-0.05)] \\ &= 39.44\% \end{aligned}$$

**Question 14.** (4 marks) An invoice for \$1 000 dated June 13<sup>th</sup> with terms 5/15 E.O.M. is received with the goods on June 17<sup>th</sup>. What amount must be paid on July 11<sup>th</sup> to reduce the debt to \$500.

Since July 11<sup>th</sup> is within the discount period

$$500(0.95) = \$475$$

must be paid.

**Question 15. (4 marks)**

The Pink Book Store sells the book Das Kapital for \$43.33. The markup is 10% of the cost. What is the cost of the book? What is the rate of markup based on selling price?

$$\begin{aligned}
 S &= C + M \\
 43.33 &= C + 10\% \text{ of } C \\
 43.33 &= C + 0.1C \\
 43.33 &= 1.1C \\
 \$39.39 &= C
 \end{aligned}$$

$$\begin{aligned}
 \text{rate of markup based} &= \frac{S-C}{S} \\
 \text{on selling price} &= \frac{43.33 - 39.39}{43.33} \\
 &= 9.09\%
 \end{aligned}$$

**Question 16. (6 marks)**

The Kunming DVD Store paid \$0.55 for a DVD. Expenses are 33% of selling price and the required profit is 11% of the selling price. The older DVDs are marked down 30%. What is the regular selling price of a DVD? What is the selling price of a marked down DVD? What is the operating loss or profit on the older DVDs?

$$\begin{aligned}
 S &= C + E + P \\
 S &= 0.55 + 33\% \text{ of } S + 11\% \text{ of } S \\
 S &= 0.55 + 0.33S + 0.11S \\
 S &= 0.55 + 0.44S \\
 0.56S &= 0.55 \\
 S &= \$0.98
 \end{aligned}$$

$$\begin{aligned}
 \text{Profit} &= \text{Sale price} - \text{Total Cost} \\
 &= 0.69 - 0.87 \\
 &= \$ -0.18
 \end{aligned}$$

$$\begin{aligned}
 \text{Sale price} &= (1 - 0.30) 0.98 \\
 &= \$0.69
 \end{aligned}$$

∴ an operating loss  
of \$ -0.18

$$\begin{aligned}
 \text{Total Cost} &= C + E \\
 &= 0.55 + 0.33 \\
 &= 0.55 + 0.33(0.98) \\
 &= \$0.87
 \end{aligned}$$

**Question 17. (6 marks)**

The local camera store paid \$1 700.00 for a Nikon lens less 30%, 10% and 5%. Overhead expenses are 15% of the regular selling price and profit is 5% of the regular selling price. During a sale the lens was sold at a markdown of 15%. What was the operating profit or loss on the sale?

$$\begin{aligned}
 C &= N = (1-d_1)(1-d_2)(1-d_3)L \\
 &= (1-30\%)(1-10\%)(1-5\%)1700.00 \\
 &= (0.70)(0.90)(0.95)1700.00 \\
 &= \$1017.45
 \end{aligned}$$

$$\begin{aligned}
 S &= C + E + P \\
 S &= 1017.45 + 15\% \text{ of } S + 5\% \text{ of } S \\
 S &= 1017.45 + 0.15S + 0.05S \\
 0.8S &= 1017.45 \\
 S &= \$1271.81
 \end{aligned}$$

$$\begin{aligned}
 \text{Sale price} &= (1-15\%)(1271.81) \\
 &= \$1081.04
 \end{aligned}$$

∴ an operating loss of -127.18.

$$\begin{aligned}
 \text{Total Cost} &= C + E \\
 &= 1017.45 + 0.15S \\
 &= 1017.45 + 190.77 \\
 &= \$1208.22
 \end{aligned}$$

$$\begin{aligned}
 \text{Profit} &= \text{Sale price} - \text{Total Cost} \\
 &= 1081.04 - 1208.22 \\
 &= \$127.18
 \end{aligned}$$

**Bonus Question (2 marks)**

Find 3 consecutive integers such that 3 times the smallest less 10 is 9 more than the sum of the other two.

$$\begin{aligned}
 \text{first integer} &\rightarrow x & 3x - 10 &= [(x+1) + (x+2)] + 9 \\
 \text{second integer} &\rightarrow x+1 & 3x - 10 &= [2x+3] + 9 \\
 \text{third integer} &\rightarrow x+2 & 3x - 10 &= 2x + 12 \\
 & & x &= 22
 \end{aligned}$$

∴ The 3 consecutive integers are 22, 23, 24