

Quiz 2

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. §5.4#87 (5 marks)

Integrate the following indefinite integral:

$$\int \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$$

① $\int \frac{e^u}{\sqrt{x}} dx$

Let $u = \sqrt{x}$ ①
 $\Rightarrow du = u'(x) dx$
 $du = \frac{1}{2\sqrt{x}} dx$
 $2du = \frac{1}{\sqrt{x}} dx$ ②

② $\int e^u \cdot 2 \cdot du$

$= 2 \int e^u du$

$= 2e^u + C$

\rightarrow ① $= 2e^{\sqrt{x}} + C$

Question 2. §5.7#13 (5 marks)

Integrate the following indefinite integral:

$$\int \frac{e^{2x}}{4 + e^{4x}} dx$$

Let $u = e^{2x}$ ①
 $\Rightarrow du = u'(x) dx$
 $du = 2e^{2x} dx$
 $\frac{du}{2} = e^{2x} dx$ ②

$= \int \frac{e^{2x}}{4 + (e^{2x})^2} dx$

① $\int \frac{e^{2x}}{2^2 + u^2} dx$

② $\int \frac{1}{2^2 + u^2} \cdot \frac{du}{2}$

$= \frac{1}{2} \int \frac{1}{2^2 + u^2} du$

$= \frac{1}{2} \left[\frac{1}{2} \arctan \frac{u}{2} \right] + C$

① $= \frac{1}{4} \arctan \frac{e^{2x}}{2} + C$