

Quiz 3

Question 1. (4 marks) Determine which of the following expressions are defined for the matrices

$$A_{4 \times 5} \quad B_{4 \times 5} \quad C_{5 \times 2} \quad D_{4 \times 2} \quad E_{5 \times 4}$$

For those that are defined give the size (dimensions) of the resulting matrix.

a) $AC+D$ 4×2

b) $E(AC)$ 5×2

c) $E^T A$ UNDEFINED

d) $E(A+B)$ 5×5

Question 2. (6 marks)

$$\text{Given: } A = \begin{bmatrix} 3 & 0 \\ -1 & 2 \\ 1 & 1 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 5 \\ -1 & 0 \end{bmatrix} \quad C = \begin{bmatrix} 6 & 1 \\ -1 & 1 \end{bmatrix}$$

Find:

a) $C-B = \begin{bmatrix} 6 & 1 \\ -1 & 1 \end{bmatrix} - \begin{bmatrix} 1 & 5 \\ -1 & 0 \end{bmatrix} = \begin{bmatrix} 5 & -4 \\ 0 & 1 \end{bmatrix}$

b) $2A^T = 2 \begin{bmatrix} 3 & 0 \\ -1 & 2 \\ 1 & 1 \end{bmatrix}^T = 2 \begin{bmatrix} 3 & -1 & 1 \\ 0 & 2 & 1 \end{bmatrix} = \begin{bmatrix} 6 & -2 & 2 \\ 0 & 4 & 2 \end{bmatrix}$

c) $\frac{1}{2}(AB) = \frac{1}{2} \left(\begin{bmatrix} 3 & 0 \\ -1 & 2 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 5 \\ -1 & 0 \end{bmatrix} \right) = \frac{1}{2} \begin{bmatrix} 3 & 15 \\ -3 & -5 \\ 0 & 5 \end{bmatrix} = \begin{bmatrix} 3/2 & 15/2 \\ -3/2 & -5/2 \\ 0 & 5/2 \end{bmatrix}$