

Name: SOLUTIONS

Student ID: \_\_\_\_\_

### Quiz 9

**Question 1.** (2 marks) Find a vector normal to both  $\vec{u} = (1, -2, 3)$  and  $\vec{v} = (0, -3, 5)$ .

$$\begin{aligned}\vec{u} \times \vec{v} &= \left( \det \begin{bmatrix} 2 & 3 \\ 3 & 5 \end{bmatrix}, -\det \begin{bmatrix} 1 & 0 \\ 3 & 5 \end{bmatrix}, \det \begin{bmatrix} 1 & 0 \\ -2 & -3 \end{bmatrix} \right) \\ &= (-1, -5, -3)\end{aligned}$$

**Question 2.** (3 marks) Find the area of the parallelogram determined by the vectors  $\vec{u} = (-6, 0, 2)$  and  $\vec{v} = (2, 2, 3)$ .

$$\begin{aligned}\text{AREA} &= \|\vec{u} \times \vec{v}\| = \left\| \left( \det \begin{bmatrix} 0 & 2 \\ 2 & 3 \end{bmatrix}, -\det \begin{bmatrix} -6 & 2 \\ 2 & 3 \end{bmatrix}, \det \begin{bmatrix} -6 & 0 \\ 0 & 2 \end{bmatrix} \right) \right\| \\ &= \|(-4, 22, -12)\| = \sqrt{(-4)^2 + (22)^2 + (-12)^2} \\ &= \sqrt{644} = 2\sqrt{161} \text{ units}^2\end{aligned}$$

**Question 3.** (3 marks) Find the volume of the parallelepiped determined by the vectors  $\vec{u} = (4, 0, -1)$ ,  $\vec{v} = (3, 1, 7)$ , and  $\vec{w} = (-2, 2, 4)$ .

$$\begin{aligned}\text{Volume} &= |\vec{u} \cdot (\vec{v} \times \vec{w})| = \left| \det \begin{bmatrix} 4 & 0 & -1 \\ 3 & 1 & 7 \\ -2 & 2 & 4 \end{bmatrix} \right| \\ &= \left| 4 \det \begin{bmatrix} 1 & 7 \\ 2 & 4 \end{bmatrix} - \det \begin{bmatrix} 3 & 1 \\ -2 & 2 \end{bmatrix} \right| \\ &= \left| 4(-10) - (8) \right| = 48 \text{ units}^3\end{aligned}$$