

Last Name: SOLUTIONS

First Name: _____

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Quiz 7 (A)

Question 1. (3 marks) Given the point $Q(3, -1, 5)$ find an initial point P so that the vector \vec{PQ} is in the opposite direction as $\vec{v} = (1, -1, -2)$.

LET P BE THE POINT $P(x, y, z)$

$$\text{THEN } \vec{PQ} = (3-x, -1-y, 5-z) = -\vec{v} = (-1, 1, 2)$$

$$\Rightarrow x=4, y=-2, z=3$$

SO WE HAVE INITIAL POINT $P(4, -2, 3)$

Question 2. (3 marks) Given $\vec{u} = (1, 3, -1)$, $\vec{v} = (0, 2, 2)$, and $\vec{w} = (-3, 1, 2)$ evaluate

$$\begin{aligned} \|\vec{3u} - 2\vec{v} + \vec{w}\| & \quad \vec{3u} - 2\vec{v} + \vec{w} = 3(1, 3, -1) - 2(0, 2, 2) + (-3, 1, 2) \\ & = (3, 9, -3) - (0, 4, 4) + (-3, 1, 2) \\ & = (0, 6, -5) \end{aligned}$$

$$\therefore \|\vec{3u} - 2\vec{v} + \vec{w}\| = \sqrt{0^2 + 6^2 + (-5)^2} = \sqrt{36 + 25} = \sqrt{61}$$

Question 3. (4 marks) Find the angle between the vectors $\vec{u} = (2, -2, -4)$, and $\vec{v} = (2, 1, -1)$.

$$\vec{u} \cdot \vec{v} = \|\vec{u}\| \|\vec{v}\| \cos \theta \Rightarrow \cos \theta = \frac{\vec{u} \cdot \vec{v}}{\|\vec{u}\| \|\vec{v}\|}$$

$$\vec{u} \cdot \vec{v} = (2, -2, -4) \cdot (2, 1, -1) = 4 - 2 + 4 = 6$$

$$\|\vec{u}\| = \sqrt{2^2 + (-2)^2 + (-4)^2} = \sqrt{4 + 4 + 16} = \sqrt{24}$$

$$\|\vec{v}\| = \sqrt{2^2 + 1^2 + (-1)^2} = \sqrt{4 + 1 + 1} = \sqrt{6}$$

$$\therefore \cos \theta = \frac{6}{\sqrt{24} \sqrt{6}} = \frac{6}{\sqrt{144}} = \frac{6}{12} = \frac{1}{2}$$

$$\therefore \theta = \frac{\pi}{3}$$