

Last Name: SOLUTIONS

First Name: _____

Student ID: _____

Quiz 6

Question 1. (10 marks) The weekly demand for the pulsar 25 colour LED television is $p = 600 - 0.05x$ where p denotes the wholesale unit price in dollars and x denotes the quantity demanded. The weekly total cost function associated with manufacturing the Pulsar 25 is given by $C(x) = 0.000002x^3 - 0.03x^2 + 400x + 80000$ where $C(x)$ denotes the total cost incurred in producing x sets.

(a) Find the Revenue function and the profit function.

(b) Find the marginal cost function, marginal revenue function and marginal profit function.

(c) Evaluate the functions from part (b) at $x = 2000$ and interpret your results.

$$\begin{aligned} \text{a) } R(x) &= xp = x(600 - 0.05x) = 600x - 0.05x^2 \\ P(x) &= R(x) - C(x) = 600x - 0.05x^2 - [0.000002x^3 - 0.03x^2 + 400x + 80000] \\ &= -0.000002x^3 - 0.02x^2 + 200x - 80000 \end{aligned}$$

$$\text{b) MARGINAL COST: } C'(x) = 0.000006x^2 - 0.06x + 400$$

$$\text{MARGINAL REVENUE: } R'(x) = 600 - 0.1x$$

$$\text{MARGINAL PROFIT: } P'(x) = -0.000006x^2 - 0.04x + 200$$

$$\begin{aligned} \text{c) } C'(2000) &= 0.000006(2000)^2 - 0.06(2000) + 400 \\ &= 304 \end{aligned}$$

$$R'(2000) = 600 - 0.1(2000) = 400$$

$$\begin{aligned} P'(2000) &= -0.000006(2000)^2 - 0.04(2000) + 200 \\ &= 96 \end{aligned}$$

∴ THE COST OF PRODUCING THE 2001st T.V. IS APPROXIMATELY \$304
 THE REVENUE REALIZED FROM THE SALE OF THE 2001st T.V. IS APPROXIMATELY \$400
 THE PROFIT REALIZED FROM THE SALE OF THE 2001st T.V. IS APPROXIMATELY \$96