

Quiz 1

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. (1 mark each) Differentiate the following functions:

a.

$$f(x) = \frac{1}{x^{8/7}} = x^{-8/7} \quad f'(x) = -\frac{8}{7} x^{-15/7} = -\frac{8}{7x^{15/7}}$$

b.

$$f(x) = \cos x \quad f'(x) = -\sin x$$

c.

$$f(x) = \tan x \quad f'(x) = \sec^2 x$$

d.

$$f(x) = e^x \quad f'(x) = e^x$$

e.

$$f(x) = \csc x \quad f'(x) = -\csc x \cot x$$

f.

$$f(x) = \arcsin x \quad f'(x) = \frac{1}{\sqrt{1-x^2}}$$

Question 2. (2 marks each) Differentiate the following functions (do not simplify):

a.

$$f(x) = (\arctan x)(\operatorname{arcsec} \ln x) \quad f'(x) = \frac{1}{1+x^2} \operatorname{arcsec}(\ln x) + \arctan x \cdot \frac{1}{\ln x \sqrt{(\ln x)^2 - 1}} \cdot \frac{1}{x}$$

b.

$$f(x) = \left(\frac{\tan 3x}{\csc 2x} \right)^2$$

$$f'(x) = 2 \left(\frac{\tan 3x}{\csc 2x} \right) \left[\frac{\sec^2 3x (3) \csc(2x) - \tan 3x (-1) \csc 2x \cot 2x (2)}{(\csc 2x)^2} \right]$$