

Last Name: SOLUTIONS

First Name: _____

Student ID: _____

Quiz 6

Question 1. (5 marks) Camille purchased a 15-yr franchise for a computer outlet store that is expected to generate income at the rate of $R(t) = 400000$ dollars/year. If the prevailing interest rate is 8%/year compounded continuously, find the present value of the franchise.

$$\begin{aligned}
 PV &= \int_0^T R(t) e^{-rt} dt = \int_0^{15} 400000 e^{-0.08t} dt = 400000 \int_0^{15} e^{-0.08t} dt \\
 &= 400000 \left[\frac{e^{-0.08t}}{-0.08} \right]_0^{15} = 5000000 \left[-e^{-1.2} + e^0 \right] \\
 &= \$3\,494\,028.94
 \end{aligned}$$

Question 2. (5 marks) A state lottery commission pays the winner of the "Million Dollar" lottery 20 annual installments of \$50 000 each. If the prevailing interest rate of 6%/year compounded continuously, FIND THE PRESENT VALUE OF THE WINNING TICKET.

$$\begin{aligned}
 PV &= \frac{mP}{r} (1 - e^{-rT}) = \frac{(1)(50\,000)}{0.06} (1 - e^{-0.06(20)}) \\
 &= \$582\,338.16
 \end{aligned}$$