## **Geometric Interpretation of the Definite Integral**

Recall that, if f(x) is a continuous function, the definition of the definite integral is the following:

$$\int_{a}^{b} f(x) \, dx = \lim_{n \to \infty} \sum_{i=1}^{n} f(x_i) \Delta x$$

If f(x) is also a positive function on the interval [a,b] then this integral gives us the area under f(x) and above the *x*-axis between *a* and *b*.

But what if f(x) is not a positive function on [a,b]? What does the definite integral represent?

## **Geometri Interpretation of the Definite Integral**

If f(x) is a continuous function on [a,b] then

$$\int_{a}^{b} f(x) \, dx$$

is equal to the area above [a,b] minus the area below [a,b].

Example: Let f(x) be the function with graph

Find:

$$(\mathbf{a}) \int_0^1 f(x) \, dx$$

$$(\mathbf{b}) \ \int_0^0 f(x) \, dx$$

(c) 
$$\int_0^3 \int f(x) \, dx$$

$$(\mathbf{d}) \ \int_0^5 f(x) \, dx$$

Example: Let  $f(x) = 4 - x^2$ (a) Graph f(x)(b) Evaluate  $\int_0^2 f(x) dx$ (c) Evaluate  $\int_2^3 f(x) dx$ (d) Evaluate  $\int_0^3 f(x) dx$