

Quiz 6

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. §3.1 #75 (2 marks) Find the derivative of the function f .

$$f(x) = \frac{2}{x^2} - \frac{3}{x^{1/3}} = 2x^{-2} - 3x^{-1/3}$$

$$f'(x) = -4x^{-3} - 3\left(-\frac{1}{3}\right)x^{-4/3} = \frac{-4}{x^3} + \frac{1}{x^{4/3}}$$

Question 2. §3.2 #13 (4 marks) Find the derivative of the function f .

$$f(x) = (x^2 - 5x + 2)\left(x - \frac{2}{x}\right)$$

$$\begin{aligned} f'(x) &= \frac{d}{dx} [x^2 - 5x + 2] \left(x - \frac{2}{x}\right) + (x^2 - 5x + 2) \frac{d}{dx} \left[x - \frac{2}{x}\right] \\ &= (2x - 5)\left(x - \frac{2}{x}\right) + (x^2 - 5x + 2)\left(1 + \frac{2}{x^2}\right) \end{aligned}$$

Question 3. §3.2 #25 (4 marks) Find the derivative of the function f .

$$f(x) = \frac{x+1}{2x^2+2x+3}$$

$$\begin{aligned} f'(x) &= \frac{\frac{d}{dx} [x+1] (2x^2+2x+3) - (x+1) \frac{d}{dx} [2x^2+2x+3]}{(2x^2+2x+3)^2} \\ &= \frac{(2x^2+2x+3) - (x+1)(4x+2)}{(2x^2+2x+3)^2} \end{aligned}$$

Question 4. (2 marks) Find the exact value of:

$$\arccos\left(-\frac{\sqrt{3}}{2}\right)$$

see test #1

Question 5. (3 marks) Find the indicated limit, if it exists

$$\lim_{x \rightarrow -5} \frac{\sqrt{14+x}-3}{x+5}$$

see test #1