

Quiz 5

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. (3 marks) §6.1 #13 Evaluate the integral.

$$\begin{aligned} \int \ln(2x+1) dx &= uv - \int v du & u &= \ln(2x+1) & du &= \frac{1}{2x+1} \cdot 2 dx \\ &= x \ln(2x+1) - \int \frac{2x}{2x+1} dx & v &= x & dv &= dx \\ &= x \ln(2x+1) - \int \frac{2x+1-1}{2x+1} dx \\ &= x \ln(2x+1) - \int \frac{2x+1}{2x+1} dx + \int \frac{1}{2x+1} dx \\ &= x \ln(2x+1) - x + \frac{1}{2} \ln|2x+1| + C \end{aligned}$$

Question 2. (4 marks) §6.1 #24 Evaluate the integral.

$$\begin{aligned} I &= \int_0^t e^s \sin(t-s) ds = [uv]_0^t - \int_0^t v du & u &= e^s & du &= e^s ds \\ & & v &= \cos(t-s) & dv &= \sin(t-s) ds \\ I &= [e^s \cos(t-s)]_0^t - \int_0^t e^s \cos(t-s) ds \\ I &= e^t \cos(0) - e^0 \cos(t) - \left[[uv]_0^t - \int_0^t v du \right] & u &= e^s & du &= e^s ds \\ I &= e^t - \cos(t) - \left[[-e^s \sin(t-s)]_0^t - \int_0^t -e^s \sin(t-s) ds \right] & v &= \sin(t-s) & dv &= \cos(t-s) ds \\ I &= e^t - \cos(t) + e^t \sin(0) - e^0 \sin t - I \\ 2I &= e^t - \cos t - \sin t + C \\ I &= \frac{1}{2} [e^t - \cos t - \sin t] \end{aligned}$$

Question 3. (3 marks) §6.2 #8 Evaluate the integral.

$$\begin{aligned} \int_0^{\pi/2} \sin^2(2\theta) d\theta &= \int_0^{\pi/2} \frac{1 - \cos 4\theta}{2} d\theta \\ &= \frac{1}{2} \int_0^{\pi/2} 1 - \cos 4\theta d\theta \\ &= \frac{1}{2} \left[\theta - \frac{\sin 4\theta}{4} \right]_0^{\pi/2} = \frac{1}{2} \left[\left[\frac{\pi}{2} - \frac{\sin 4(\frac{\pi}{2})}{4} \right] - \left[0 - \frac{\sin 0}{4} \right] \right] \\ &= \frac{1}{2} \left[\left[\frac{\pi}{2} - 0 \right] - \left[0 - 0 \right] \right] = \frac{\pi}{4} \end{aligned}$$