Dawson College: Principles of Mathematics and Logic: 360-124-DW-S02: Winter 2013

Name: Student ID:

Test 1

No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. (2 marks) Give a justification for the inclusion of a course on Principles of Mathematics and Logic in the Dawson College Liberal Arts program citing historical examples from liberal education.

Question 2.¹ Given the following symbolization key:

- A: Alexander Berkman loves Emma Goldman
- B_1 : Alexander Berkman buys bread.
- B_2 : Emma Golman buys bread.
- E: Emma Goldman loves Alexander Berkman.
- F_1 : Alexander Berkman buys flowers.
- F_2 : Emma Goldman buys flowers.
- *P*₁: Alexander Berkman protests.
- P₂: Emma Goldman protests.

Translate each English language statement into Propositional Logic.

- a. (3 marks) Emma and Alexander protest only if, it is the case that both Emma buys flowers and Alexander buys bread.
- b. (3 marks) Neither Alexander loves Emma nor Emma loves Alexander if, they do not both protest.

Translate each Propositional Logic statement into English.

- c. (1 mark) $\neg F_2$
- d. (3 marks) $(\neg F_2 \lor B_1) \iff A$

Question 3. (6 marks) Determine wether the following statement is a tautology, contradiction, or contingent statement. Justify your conclusion.

 $[(A \to B) \land (B \to C))] \to (A \to C)$

Question 4. (6 marks) Determine whether the following is a valid argument. Justify your conclusion.

 $\neg F_2, (\neg F_2 \lor B_1) \iff A \therefore A$

Question 5. Which of the following is possible? If it is possible, give an example. If it is not possible, explain why.

- a. (3 marks) A valid argument, the conclusion of which is a contradiction.
- b. (3 marks) An invalid argument, the conclusion of which is a contradiction.

Bonus Question. (1 mark) Why did you choose to study in the Liberal Arts program?