

Sigma Notation

We often use sigma notation to write sums more compactly. For Example:

$$\sum_{i=1}^n f(x_i) \Delta x = f(x_1) \Delta x + f(x_2) \Delta x + f(x_3) \Delta x + \dots + f(x_n) \Delta x$$

Here's what it means

$$\sum_{i=1}^n f(x_i) \Delta x$$

Ex:

$$1) \sum_{i=1}^4 i^2$$

$$2) \sum_{i=3}^n i$$

$$3) \sum_{k=2}^7 \ln k$$

$$4) \sum_{i=1}^7 1$$

$$5) \sum_{i=3}^8 1$$

$$6) 2^3 + 3^3 + 4^3 + \dots + n^3$$

Write the following sums in expanded form

$$1) \sum_{i=1}^5 r_i$$

$$2) \sum_{n=1}^6 \frac{1}{n+1}$$

$$3) \sum_{i=4}^6 (i^3 + 1)$$

$$4) \sum_{i=1}^n i^{10}$$

$$5) \sum_{k=1}^3 k^2 i^3$$

Write the following sums in sigma notation

$$1) 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10$$

$$2) \frac{1}{2} + \frac{2}{2} + \frac{3}{2} + \dots + \frac{9}{2}$$

$$3) \frac{3}{7} - \frac{4}{8} + \frac{5}{9} - \frac{6}{10} + \dots - \frac{10}{14}$$

$$4) 2^3 + 2^4 + 2^5 + 2^6 + \dots + 2^n$$

Sigma notation rules

1) $\sum_{i=1}^n c\alpha_i$

2) $\sum_{i=1}^n (a_i \pm b_i)$

3) $\sum_{i=1}^n 1$

4) $\sum_{i=1}^n i$

5) $\sum_{i=1}^n i^2$

6) $\sum_{i=1}^n i^3$

Proof of 4)

Ex: Evaluate the following (as much as possible)

$$1) \sum_{i=1}^{\infty} i(4i^2 - 5)$$

$$2) \sum_{i=1}^{6} i(i+2)$$

$$3) \sum_{k=0}^{8} \cos(k\pi)$$

$$4) \sum_{j=-2}^{4} 2^{3-j}$$

$$5) \quad \sum_{k=1}^n 2k$$

$$6) \quad \sum_{i=1}^n (i^2 + 3i + 4)$$

$$7) \quad \sum_{i=1}^n i(i+1)(i+2)$$