

## Quiz 2

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

**Question 1.** (1 mark each) Integrate the following indefinite integrals:

a.

$$\int \frac{1}{x^{3/5}} dx = \int x^{-3/5} dx = \frac{5}{2} x^{2/5} + C$$

b.

$$\int \sec x dx = \ln |\sec x + \tan x| + C$$

c.

$$\int \cot x dx = \ln |\sin x| + C$$

d.

$$\int \frac{1}{x\sqrt{x^2-5}} dx = \frac{1}{\sqrt{5}} \operatorname{arccsc}\left(\frac{x}{\sqrt{5}}\right) + C$$

e.

$$\int \frac{1}{x} dx = \ln |x| + C$$

f.

$$\int \sin x dx = -\cos x + C$$

**Question 2.** (4 marks) §4.7 #34 Find  $f$ .

$$f''(t) = 2e^t + 3 \sin t, \quad f(0) = 0, \quad f(\pi) = 0$$

$$f'(t) = \int f''(t) dt = \int 2e^t + 3 \sin t dt = 2e^t - 3 \cos t + C$$

$$f(t) = \int f'(t) dt = \int 2e^t - 3 \cos t + C dt = 2e^t - 3 \sin t + Ct + d$$

$$f(0) = 0$$

$$0 = 2e^0 - 3 \sin(0) + C(0) + d$$

$$-2 = d$$

$$0 = f(\pi)$$

$$0 = 2e^\pi - 3 \sin \pi + C\pi - 2$$

$$C = \frac{2 - 2e^\pi}{\pi}$$

$$\therefore f(t) = 2e^t - 3 \sin t + \frac{(2 - 2e^\pi)t}{\pi} - 2$$