Dawson College: Calculus I (CHEM. TECH.): 201-NYA-05-S04: Winter 2015

Name:	
Student ID:	

## Test 1

This test is graded out of 43 marks. No books, notes, graphing calculators or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. Evaluate the following limits, if possible. Justify.

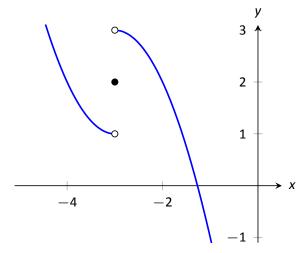
a. (2 marks)

$$\lim_{x \to -5} \frac{x^2 - x - 30}{x + 5}$$

b. (2 marks)

$$\lim_{x \to \infty} \frac{3x^3 + 2x^2 + x}{99x^3 + 1}$$

c. (2 marks) Determine the values of x for which the function, as represented below by the graph 1 doest not have a limit. Justify.



<sup>&</sup>lt;sup>1</sup>from APEX Calculus

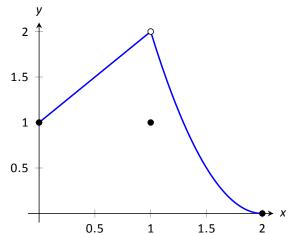
**Question 2.** (5 marks) Use the limit definition of the derivative to find the derivative of the function:

$$f(x) = \frac{x+1}{x}$$

## Question 3.

a. (2 marks) State the conditions for a function, f(x), to be continuous at x = a.

b. (2 marks) Determine the values of x for which the function, as represented below by the graph<sup>2</sup> is not continuous. Justify.



**Question 4.** Let  $f(x) = x^2 - x - 6$ .

- a. (2 marks) Find the equation of the tangent to the curve f(x) at x = 4.
- b. (1 mark) Find the equation of the normal to the curve f(x) at x = 2.
- c. (3 marks) Sketch the graph of f(x) and the tangent from part a. and the normal from part b.

**Question 5.** Find the derivative of the following functions:

a. (3 marks)

$$h(t) = \frac{t^2 + t^{3/2} + \sqrt{t} + 1}{t}$$

b. (3 marks)

$$f(z) = (z^3 + z^2)^2 (z^3 + z^2 + 1)^3$$

c. (3 marks)

$$y(x) = \sqrt{\frac{x^2 + 1}{x^3 + 1}}$$

**Question 6.** (3 marks) The Dawson chemistry students are experimenting with a new ultra fun compound called Mathemathium. While making some yields they discover that the concentration of the compound can be described by

$$C(t) = \frac{t^3 + t + \pi}{t + e}$$

in mol/L and where t is time in seconds. What is the instantaneous rate of change of concentration after 2 minutes.

**Question 7.** (5 marks) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  for the relation

$$x^2 - xy = 1 - y^2$$

## Bonus.

- a. (3 marks) Why does Newton's Method fail in finding a root of  $f(x) = 2x^3 9x^2 + 12x + 6$  when  $x_0 = 1$ ? Give a geometrical justification.
- b. (2 marks) Why does Newton's Method fail in finding a root of  $f(x) = x^2 + x + 1$ .