

Quiz 4

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. (5 marks) §5.3 #29 Evaluate the integral.

$$\int_{-1}^2 (x - 2|x|) dx$$

$$\begin{aligned} &= \int_{-1}^2 x dx - 2 \int_{-1}^2 |x| dx \\ &= \left[\frac{x^2}{2} \right]_{-1}^2 - 2 \left[\int_{-1}^0 |x| dx + \int_0^2 |x| dx \right] \\ &= \frac{2^2}{2} - \frac{(-1)^2}{2} - 2 \left[\int_{-1}^0 -x dx + \int_0^2 x dx \right] \\ &= 2 - \frac{1}{2} - 2 \left[\left[-\frac{x^2}{2} \right]_{-1}^0 + \left[\frac{x^2}{2} \right]_0^2 \right] \\ &= 2 - \frac{1}{2} - 2 \left[\frac{(-1)^2}{2} + \frac{2^2}{2} \right] \\ &= \frac{3}{2} - 2 \left[\frac{5}{2} \right] = -\frac{7}{2} \end{aligned}$$

Question 2. (5 marks) §5.4 #24 If $f(x) = \int_0^{\sin x} \sqrt{1+t^2} dt$ and $g(y) = \int_3^y f(x) dx$, find $g''(\pi/6)$.

$$g'(y) = f(y) \text{ by 2nd FTC}$$

$$g''(y) = f'(y)$$

$$\text{and since } f(x) = h(c(x)) \text{ where } h(x) = \int_0^x \sqrt{1+t^2} dx$$

$$c(x) = \sin x$$

$$f'(x) = h'(c(x)) c'(x) \text{ where } h'(x) = \sqrt{1+x^2} \text{ by 2nd FTC}$$

$$= \sqrt{1+\sin^2 x} \cos x$$

$$c'(x) = \cos x$$

$$g''(\pi/6) = \sqrt{1+\sin^2(\pi/6)} \cos \frac{\pi}{6}$$

$$= \sqrt{1+(\frac{1}{2})^2} \frac{\sqrt{3}}{2} = \sqrt{\frac{5}{4}} \cdot \frac{\sqrt{3}}{2} = \frac{\sqrt{15}}{4}$$