

Quiz 3

This quiz is graded out of 13 marks. No books, watches, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. (3 marks) Find all matrices A , if any, such that

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} A = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Question 2.¹ (4 marks) Solve for X when:

$$\begin{bmatrix} -13 & 1 \\ 27 & 2 \end{bmatrix} X = \begin{bmatrix} -11 & \frac{1}{2} \\ 29 & 1 \end{bmatrix} X - \begin{bmatrix} -1 & 0 \\ 2 & 2 \end{bmatrix}$$

Question 3. (2 marks) Determine whether the statement is true or false, and justify your answer.
The sum of two invertible matrices of the same size must be invertible.

Question 4. (4 marks) Show that if R is a $1 \times n$ matrix and C is an $n \times 1$ matrix, then $RC = \text{tr}(CR)$.

¹From the Fall 2017 Dawson College Final Examination.