

No books, watches, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work.

Question 1. (5 marks) Using vectors prove that the line segment joining the midpoints of two sides of a triangle is parallel to the third side and half as long.

Question 2. (5 marks) Prove the parallelogram law for the norm:

$$\|\vec{a} + \vec{b}\|^2 + \|\vec{a} - \vec{b}\|^2 = 2\|\vec{a}\|^2 + 2\|\vec{b}\|^2$$

for all vectors in \mathbb{R}^n .

Question 3. Given the line $y = x + 2$ which is a tangent of the circle with centre C . The vector \vec{v} has initial point C and terminal point B which lies both on the circle and the tangent.

note: A tangent to a circle is perpendicular to the radius at the point at which the tangent and circle intersect.

- (1 mark) Find the centre C of the circle.
- (4 marks) Find the point B .
- (1 mark) Find the equation of the circle.

