Question 1. (4 marks) Evaluate the definite integral.

$$
\int_{0}^{4} \frac{x}{\sqrt{1+2 x}} d x
$$

Question 2. (3 marks) If $a$ and $b$ are positive numbers, show that

$$
\int_{0}^{1} x^{a}(1-x)^{b} d x=\int_{0}^{1} x^{b}(1-x)^{a} d x
$$

Question 3. (4 marks) Evaluate the integral
$\int \cos (\ln x) d x$

Question 4. (3 marks) If $f(0)=g(0)=0$ and $f^{\prime \prime}$ and $g^{\prime \prime}$ are continuous, show that

$$
\int_{0}^{a} f(x) g^{\prime \prime}(x) d x=f(a) g^{\prime}(a)-f^{\prime}(a) g(a)+\int_{0}^{a} f^{\prime \prime}(x) g(x) d x
$$

