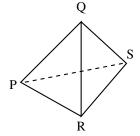
**Question 1.** (5 marks) Let P, Q, R, and S be four points, not all on one plane, as in the diagram. Show that the volume of the pyramid they determine is  $\frac{1}{6}[\vec{PQ} \cdot (\vec{PR} \times \vec{PS})]$ . Hint: The volume of a pyramid with base area A and height h is  $\frac{1}{3}Ah$ .



## Question 2.

a. (3 marks) Show that  $\mathbf{w} \cdot (\mathbf{u} \times \mathbf{v}) = \mathbf{u} \cdot (\mathbf{v} \times \mathbf{w}) = \mathbf{v} \cdot (\mathbf{w} \times \mathbf{u})$  holds for all vectors  $\mathbf{w}$ ,  $\mathbf{u}$ , and  $\mathbf{v}$ .

b. (3 marks) Show that  $\mathbf{v} - \mathbf{w}$  and  $(\mathbf{u} \times \mathbf{v}) + (\mathbf{v} \times \mathbf{w}) + (\mathbf{w} \times \mathbf{u})$  are orthogonal.