

Books, watches, notes or cell phones are **not** allowed. The **only** calculators allowed are the Sharp EL-531\*\*\*. You **must** show all your work, the correct answer is worth 1 mark the remaining marks are given for the work.

**Question 1.**<sup>1</sup> (1 mark each) Complete each of the following sentences with **MUST**, **MIGHT**, or **CANNOT**.

- Let  $A$  be a square matrix such that not all entries are zero. All entries of  $AA$  \_\_\_\_\_ be equal to zero.
- If  $B$  has a column of zeros and the product  $AB$  is defined then  $AB$  \_\_\_\_\_ have a column of zeros.
- If  $A$  has a row of zeros and the product  $AB$  is defined then  $AB$  \_\_\_\_\_ have a row of zeros.

**Question 2.**(4 marks) Find **all** matrices  $A$  where

$$A + 3A^T = \begin{bmatrix} 12 & 2 \\ -10 & 4 \end{bmatrix}$$

**Question 3.**(3 marks) Prove: If  $AB$  and  $BA$  are both defined, then  $AB$  and  $BA$  are square matrices.

---

<sup>1</sup> From or modified from a John Abbott final examination