

Question 1. Consider the lines $\mathcal{L} : \begin{cases} x = kt + 7 \\ y = t - 3 \\ z = 3t + 4 \end{cases}, t \in \mathbb{R}$ and the plane $\mathcal{P} : 3x + 4z = 7$

a. (3 marks) Determine the values of k , if any, for which \mathcal{L} is parallel to \mathcal{P} .

b. (5 marks) If such a k value exists, find the distance from the line \mathcal{L} to the plane \mathcal{P} using projections.

Question 2. (3 marks) Determine whether the following statement is true or false. If the statement is false provide a counterexample. If the statement is true provide a proof of the statement.

If \mathbf{x}_1 and \mathbf{x}_2 are two solutions of the nonhomogeneous linear system $A\mathbf{x} = \mathbf{b}$, then $\mathbf{x}_1 - \mathbf{x}_2$ is a solution of the corresponding homogeneous linear system.

Question 3. (2 marks) Find the parametric equation of the plane $x + 2y + 3z = 4$.

Question 4. (3 marks) Consider the system with equations: $x + y + z = b_1$, $x + 2y + cz = b_2$ and $x + 3y + dz = b_3$ where b_1, b_2, b_3, c, d are fixed real values, $P(1, 1, 1)$ satisfies all three equations and the solution set of the corresponding homogeneous linear system is $\mathbf{x} = t(2, -1, -1)$ where $t \in \mathbb{R}$.

Using a clearly labelled sketch give a geometrical interpretation of the linear system and its solution set, and the corresponding homogeneous linear system and its solution set.