

Books, watches, notes or cell phones are **not** allowed. The **only** calculators allowed are the Sharp EL-531\*\*\*. You **must** show all your work, the correct answer is worth 1 mark the remaining marks are given for the work.

**Question 1.** (3 marks each) Determine whether the following statements are true or false. If a statement is false provide a counterexample. If it is true provide a proof.

a. If  $A^4 = 2I$ , then the matrix  $A$  is invertible.

b. If  $AB = B$  and  $B$  is a nonzero matrix, then the matrix  $A$  is invertible.

**Question 2.** (4 marks) Solve for the matrix  $X$  if  $AX(D + BX)^{-1} = C$ . Assume that all matrices are  $n \times n$  and invertible as needed.

**Question 3.** (5 marks) Let  $B^{-1}A = \begin{bmatrix} 1 & 2 & 1 \\ 1 & 1 & 1 \\ 2 & 1 & 1 \end{bmatrix}$  and  $BX^{-1}A^{-1} = I_3$ . Find the matrix  $X$ .

**Question 4.** (5 marks) Express the above  $B^{-1}A$  as a product of elementary matrices, if possible.